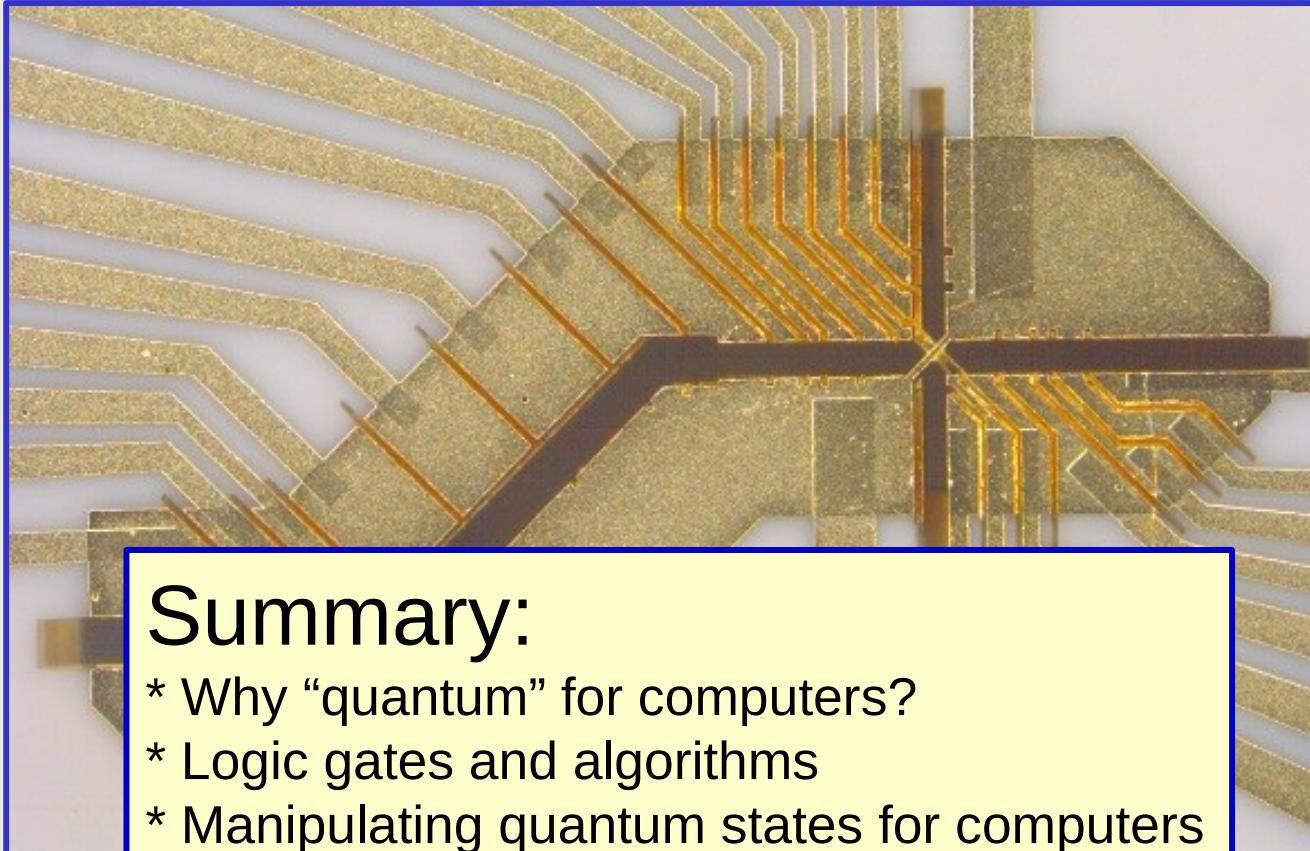


Elements of quantum information processing and quantum computers

(with trapped ion examples)

D. J. Wineland, Dept. of Physics, U Oregon, Eugene, OR;
& Research Associate, NIST, Boulder, CO



e quantum computer

Data storage:

- classical: computer bit: (0) or (1)
- quantum: “qubit” $\Psi = \alpha_0|0\rangle + \alpha_1|1\rangle$
superposition: $|0\rangle$ **AND** $|1\rangle$

Scaling: Consider 3-bit register ($N = 3$):

Classical register: (example): (101)

Quantum register: (3 qubits):

$$\Psi = \alpha_0|0,0,0\rangle + \alpha_1|0,0,1\rangle + \alpha_2|0,1,0\rangle + \alpha_3|1,0,0\rangle + \alpha_4|0,1,1\rangle + \alpha_5|1,0,1\rangle + \alpha_6|1,1,0\rangle + \alpha_7|1,1,1\rangle$$

(represents 2^3 numbers simultaneously)

For $N = 300$ qubits, store $2^{300} \approx 10^{90}$ numbers simultaneously
(more than all the classical information in universe!)

Parallel processing: single gate operates on all 2^N inputs simultaneously

e quantum computer

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measurement:

$\alpha_0|0\rangle + \alpha_1|1\rangle$ “collapses” to
 $|0\rangle$ **OR** $|1\rangle$

with probabilities $|\alpha_0|^2$ and $|\alpha_1|^2$

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Classical register: (example): (101)

Quantum register: (3 qubits):

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But!: quantum measurement rule: measured register gives only one number

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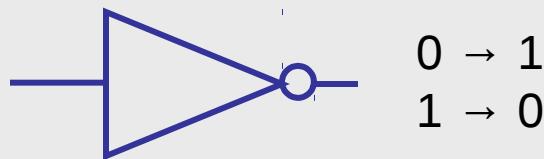
But!: quantum measurement rule: measured register gives only one number

Factoring: Peter Shor’s Algorithm (1994)

Logic gates for Universal computation

- Classical:

1-bit NOT



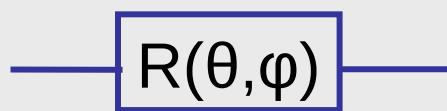
2-bit AND



| |
|--------------------|
| $00 \rightarrow 0$ |
| $01 \rightarrow 0$ |
| $10 \rightarrow 0$ |
| $11 \rightarrow 1$ |

- Quantum:

“rotation”

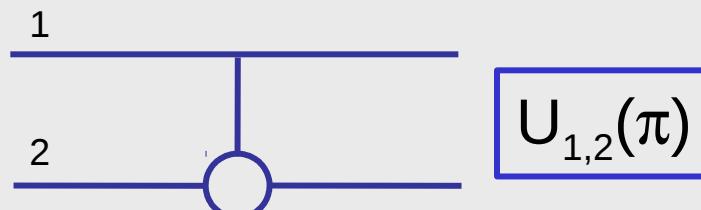


e.g.,

$$|0\rangle \rightarrow \cos(\theta/2)|0\rangle + e^{i\phi}\sin(\theta/2)|1\rangle$$
$$|1\rangle \rightarrow -e^{-i\phi}\sin(\theta/2)|0\rangle + \cos(\theta/2)|1\rangle$$

like rotating a spin-1/2 particle states: $|\downarrow\rangle$ ($= |0\rangle$) and $|\uparrow\rangle$ ($= |1\rangle$)

2-qubit logic gate



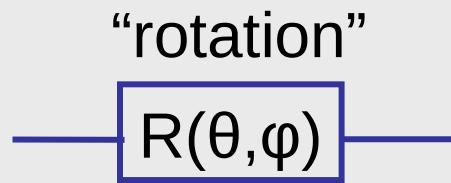
$$|0\rangle|0\rangle \rightarrow |0\rangle|0\rangle$$
$$|0\rangle|1\rangle \rightarrow |0\rangle|1\rangle$$
$$|1\rangle|0\rangle \rightarrow |1\rangle|0\rangle$$
$$|1\rangle|1\rangle \rightarrow -|1\rangle|1\rangle$$

phase gate

Universal logic gates for processing

• $\Psi = \psi_1 \otimes \psi_2 = \frac{1}{2}(|0\rangle + |1\rangle)(|0\rangle + |1\rangle) \rightarrow U_{1,2}(\pi) \rightarrow$
 $\frac{1}{2}(|0\rangle|0\rangle + |0\rangle|1\rangle + |1\rangle|0\rangle - |1\rangle|1\rangle) \neq \psi_1 \otimes \psi_2$ entanglement!

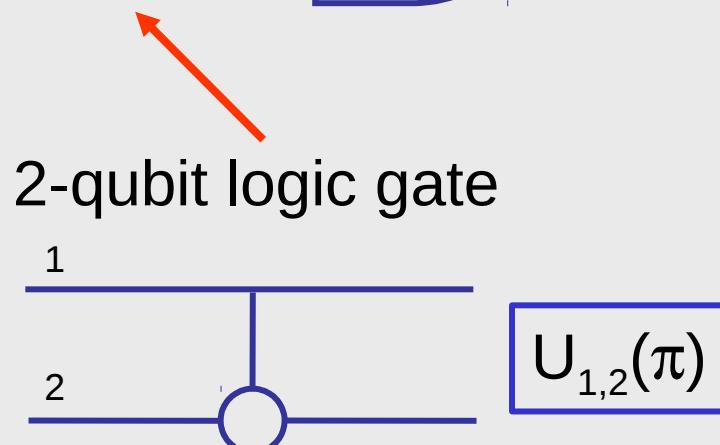
Quantum:



e.g.,

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like rotating a spin-1/2 particle states: $|\downarrow\rangle$ ($= |0\rangle$) and $|\uparrow\rangle$ ($= |1\rangle$)



$$|0\rangle|0\rangle \rightarrow |0\rangle|0\rangle$$
$$|0\rangle|1\rangle \rightarrow |0\rangle|1\rangle$$
$$|1\rangle|0\rangle \rightarrow |1\rangle|0\rangle$$
$$|1\rangle|1\rangle \rightarrow -|1\rangle|1\rangle$$

phase gate

Quantum computer algorithm to efficiently factorize large numbers

Peter Shor
(1994)

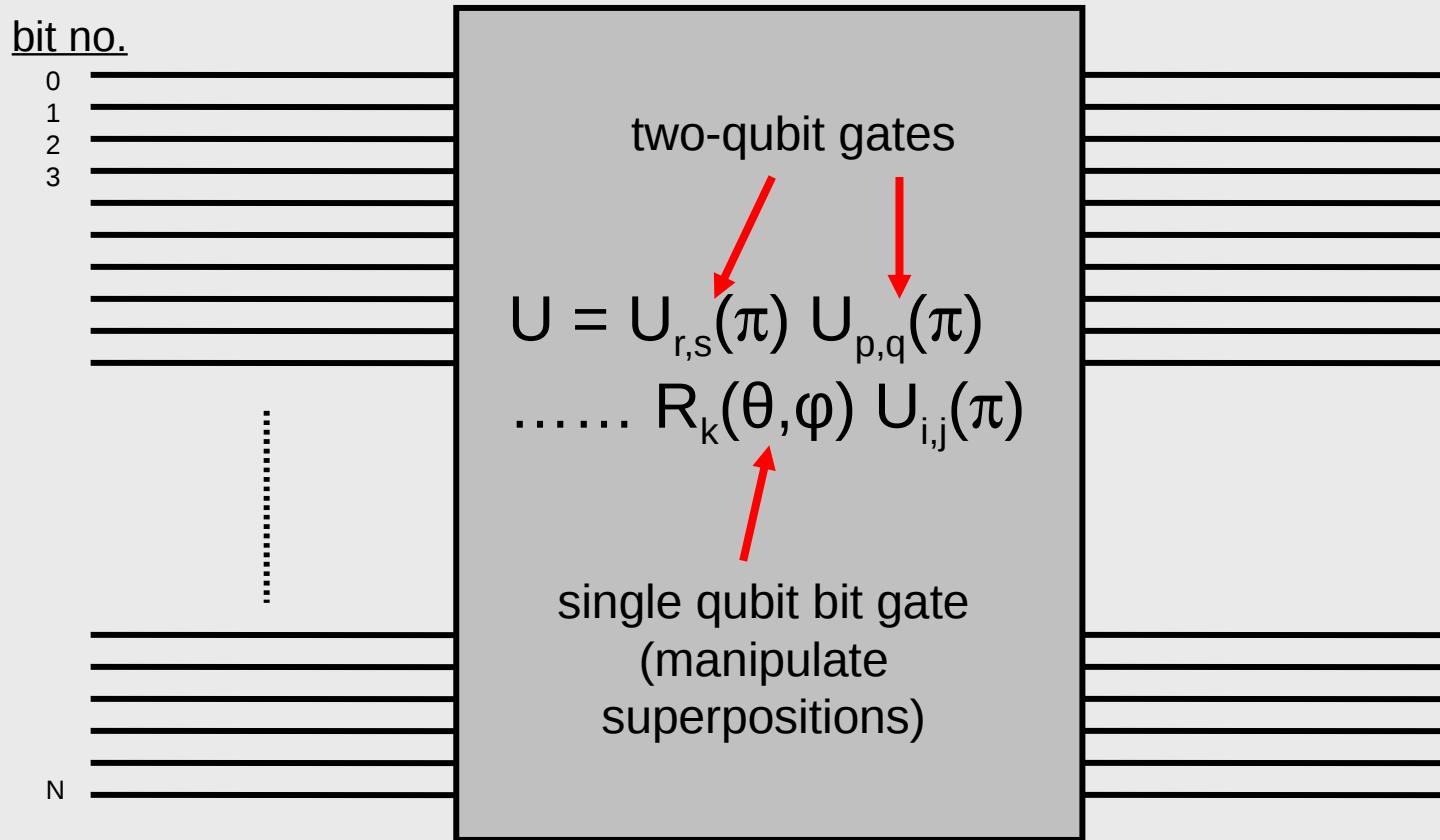


N-qubits:

$$\Psi_{in} = \sum_{i=0}^{2^N-1} |i\rangle$$

e.g., for N = 3, $\Psi_{in} = C_N [|0,0,0\rangle + |0,0,1\rangle + |0,1,0\rangle + |1,0,0\rangle + |0,1,1\rangle + |1,0,1\rangle + |1,1,0\rangle + |1,1,1\rangle]$

Process all inputs simultaneously



Quantum computer algorithm to efficiently factorize large numbers

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N-qubits:

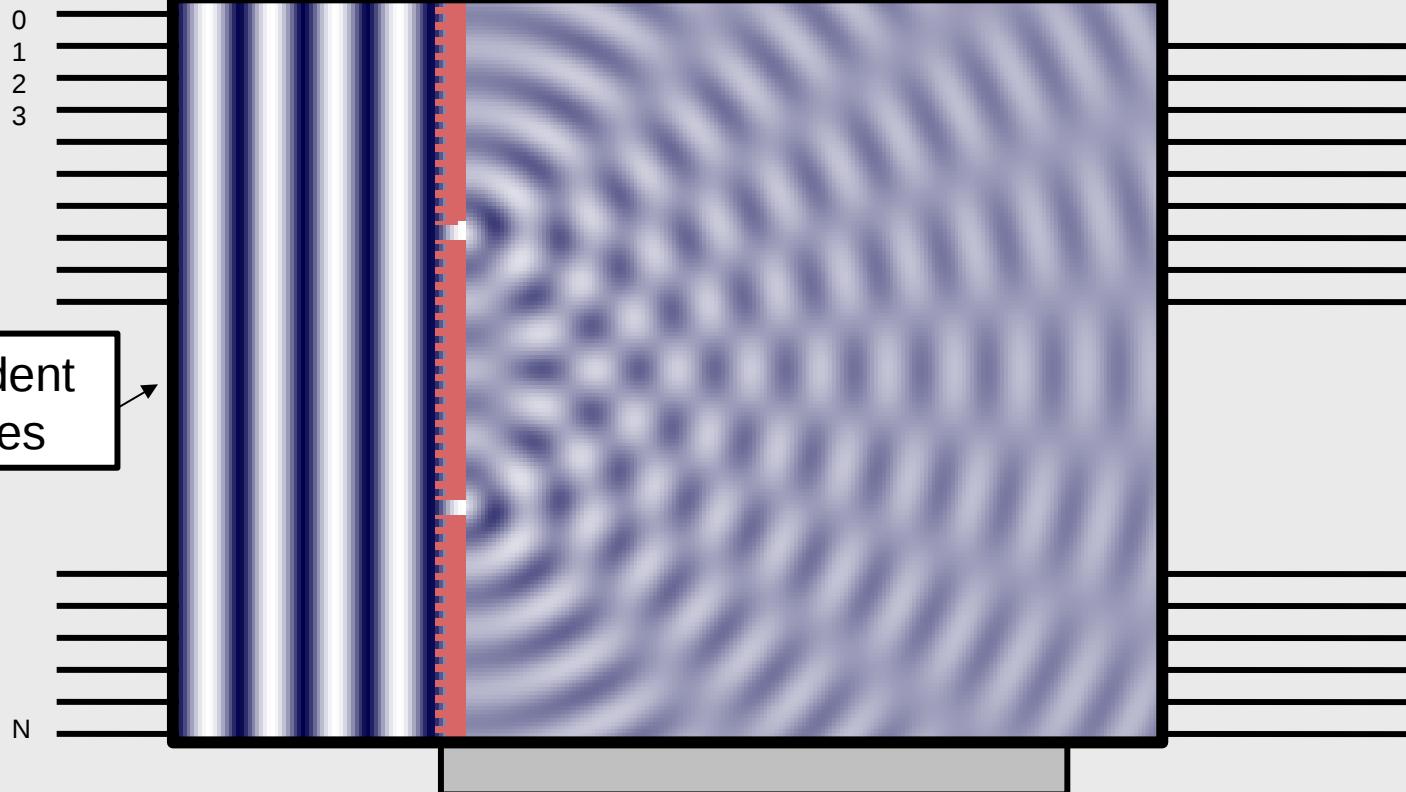
$$\Psi_{in} = \sum_{i=0}^{2^N-1} |i\rangle$$

e.g., for N = 3, $\Psi_{in} = C_N [|0,0,0\rangle + |0,0,1\rangle + |0,1,0\rangle + |1,0,0\rangle + |0,1,1\rangle + |1,0,1\rangle + |1,1,0\rangle + |1,1,1\rangle]$

Process all inputs simultaneously

analogous to
waterwave interference
(photo,Hannover Univ.)

bit no.



Quantum computer algorithm to efficiently factorize large numbers

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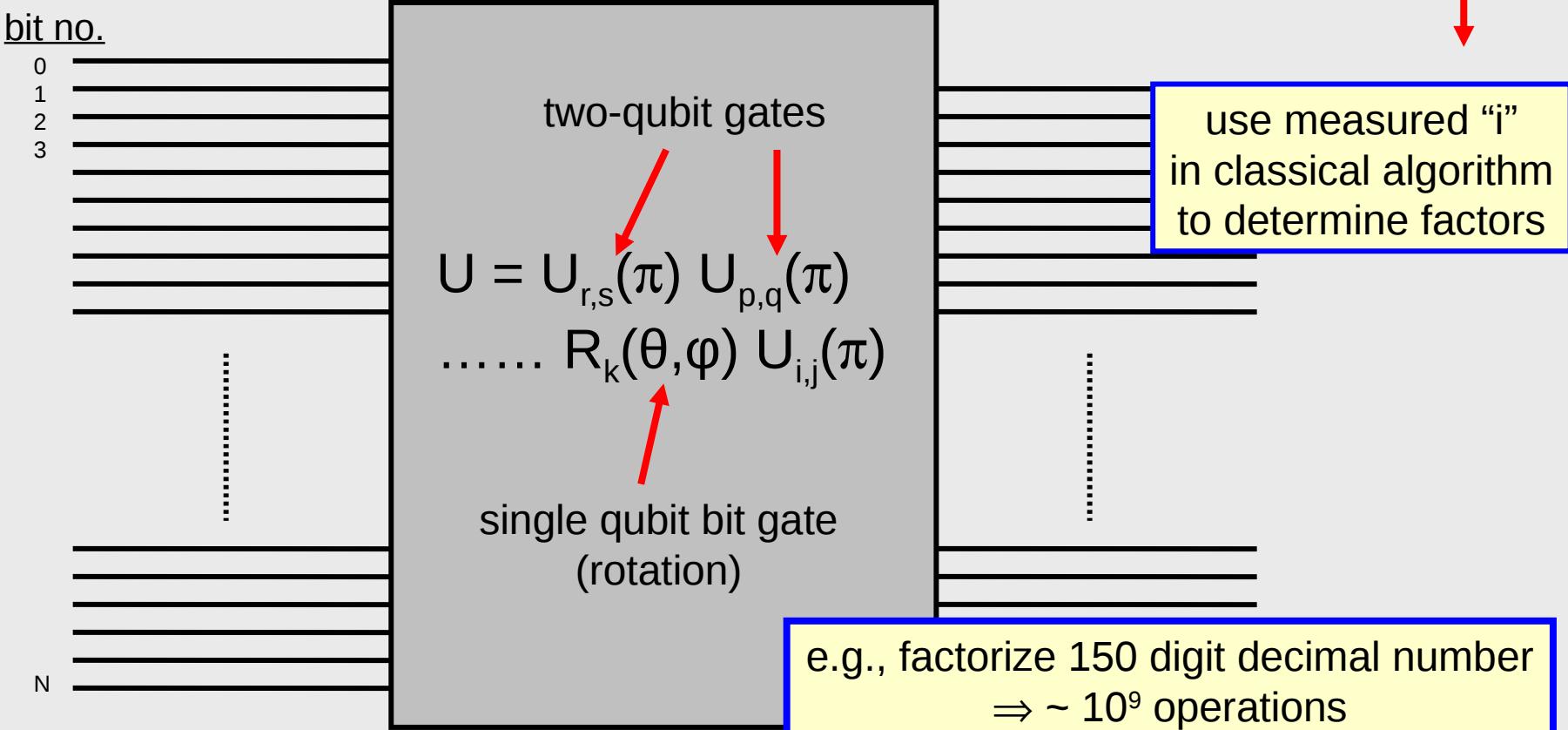


$$\Psi_{\text{in}} = \sum_{i=0}^{2^N-1} |i\rangle$$

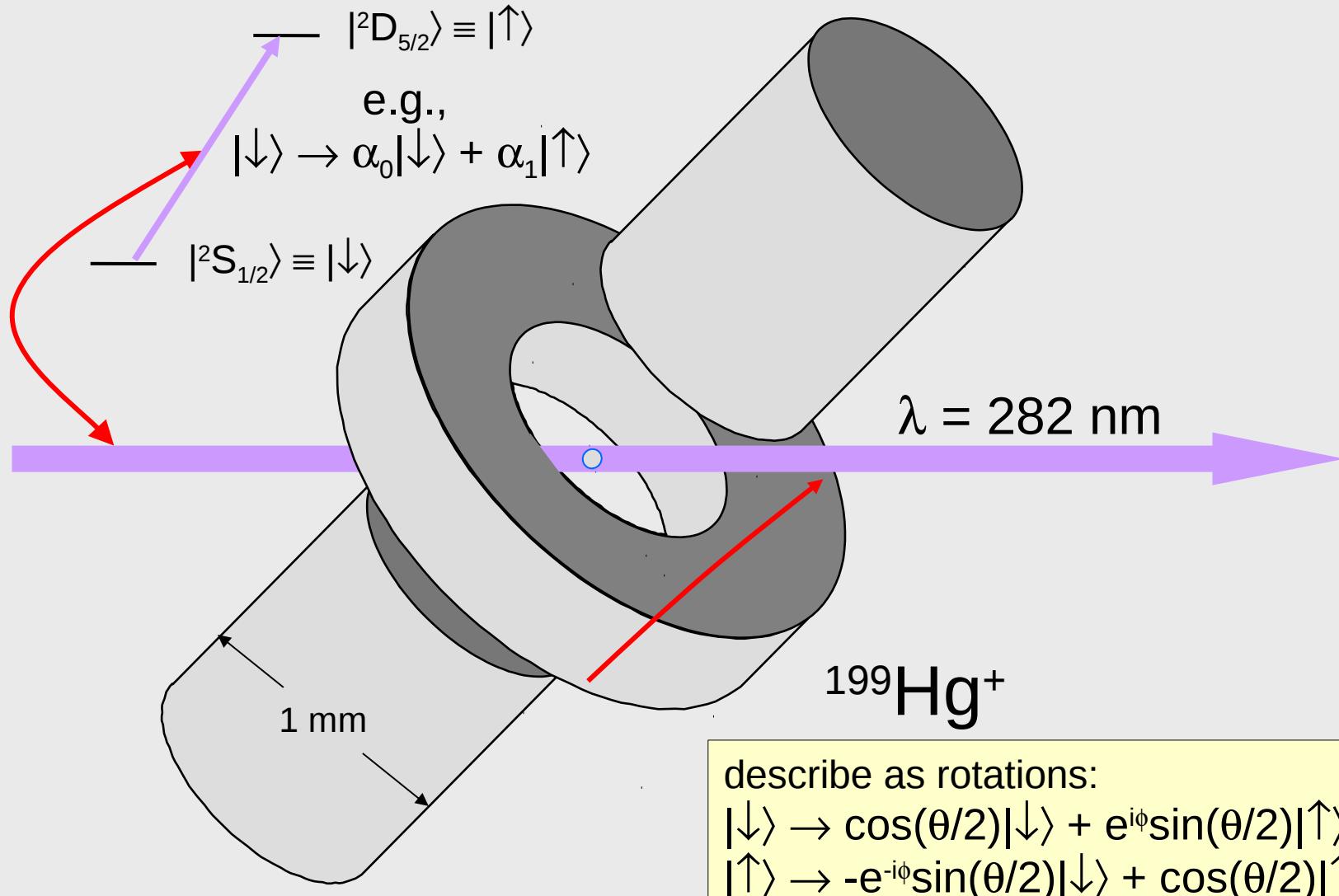
Process all possible
inputs simultaneously

$$\Psi_{\text{out}} = \sum_{\text{small selection}} |i\rangle$$

measure
qubits

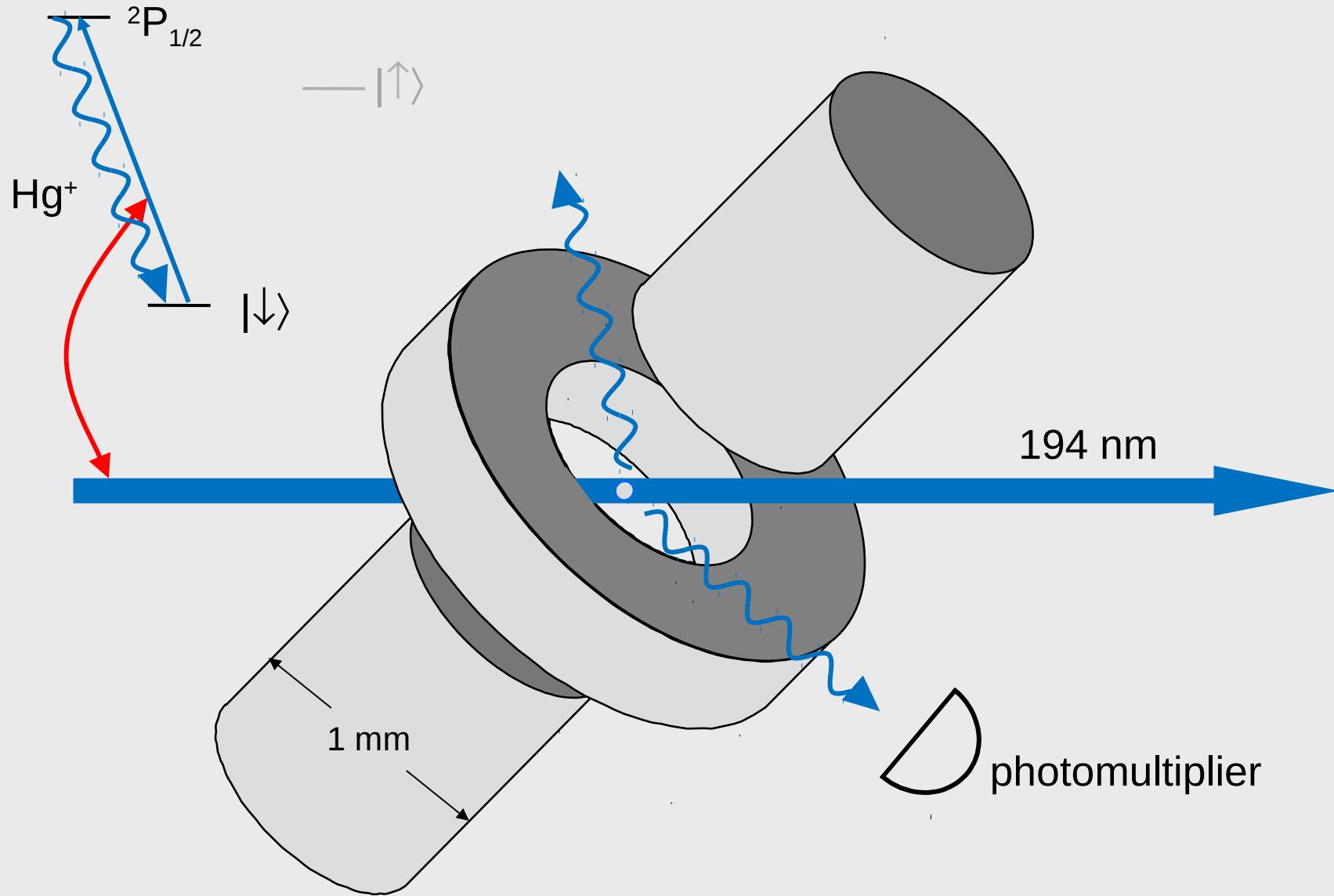


“spin” rotations (superpositions of internal energy states of ion)

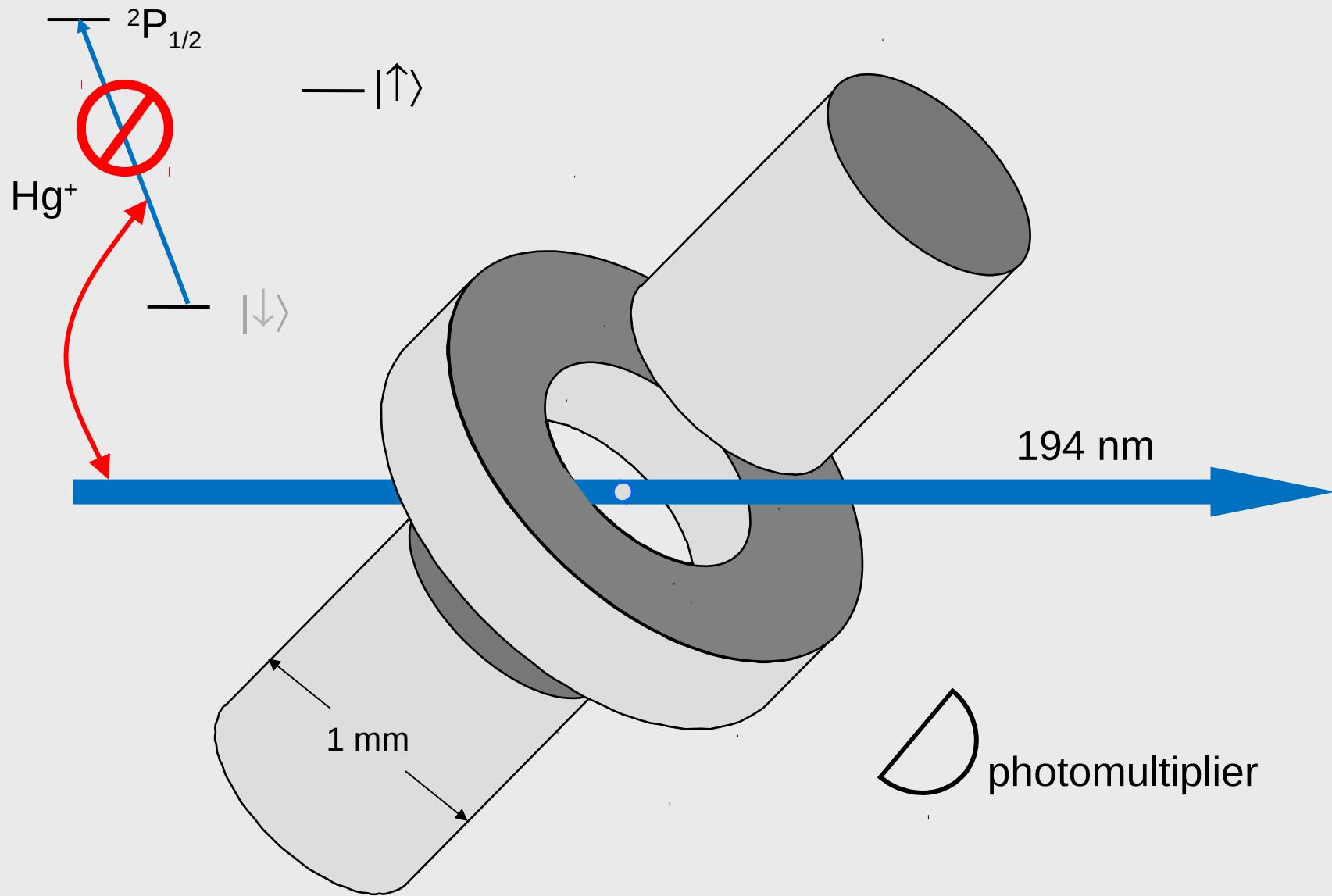


detection:

$$\alpha_0 |\downarrow\rangle + \alpha_1 |\uparrow\rangle \rightarrow |\downarrow\rangle$$



$$\alpha_0 |\downarrow\rangle + \alpha_1 |\uparrow\rangle \rightarrow |\uparrow\rangle$$



Hyperfine qubits: e.g. ${}^9\text{Be}^+$

${}^2\text{P}_{3/2}$ _____

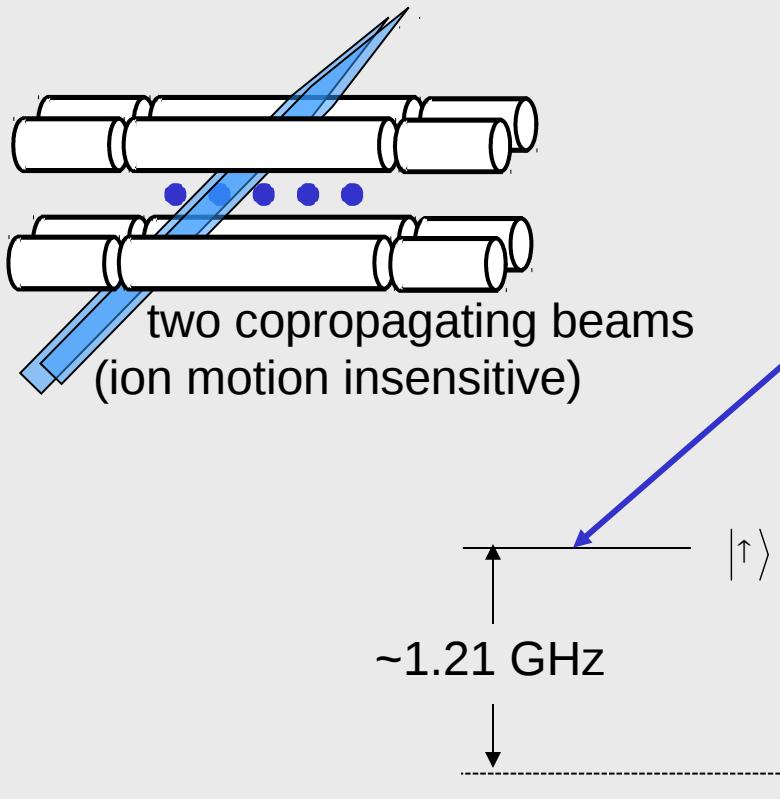
${}^2\text{S}_{1/2}$ electronic ground level

hyperfine states

$$|\downarrow\rangle \equiv |F = 2, m_F = 0\rangle$$

$$|\uparrow\rangle \equiv |F = 1, m_F = -1\rangle$$

$B \approx 119$ G (coherence time > 10 s)



${}^2\text{P}_{1/2}$ _____

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two-photon coherent
stimulated-Raman
transitions
• focused beams
 \Rightarrow individual ion
addressability

e.g., rotations

$$|\downarrow\rangle \rightarrow \cos(\theta/2)|\downarrow\rangle + e^{i\phi}\sin(\theta/2)|\uparrow\rangle$$

$$|\uparrow\rangle \rightarrow -e^{-i\phi}\sin(\theta/2)|\downarrow\rangle + \cos(\theta/2)|\uparrow\rangle$$

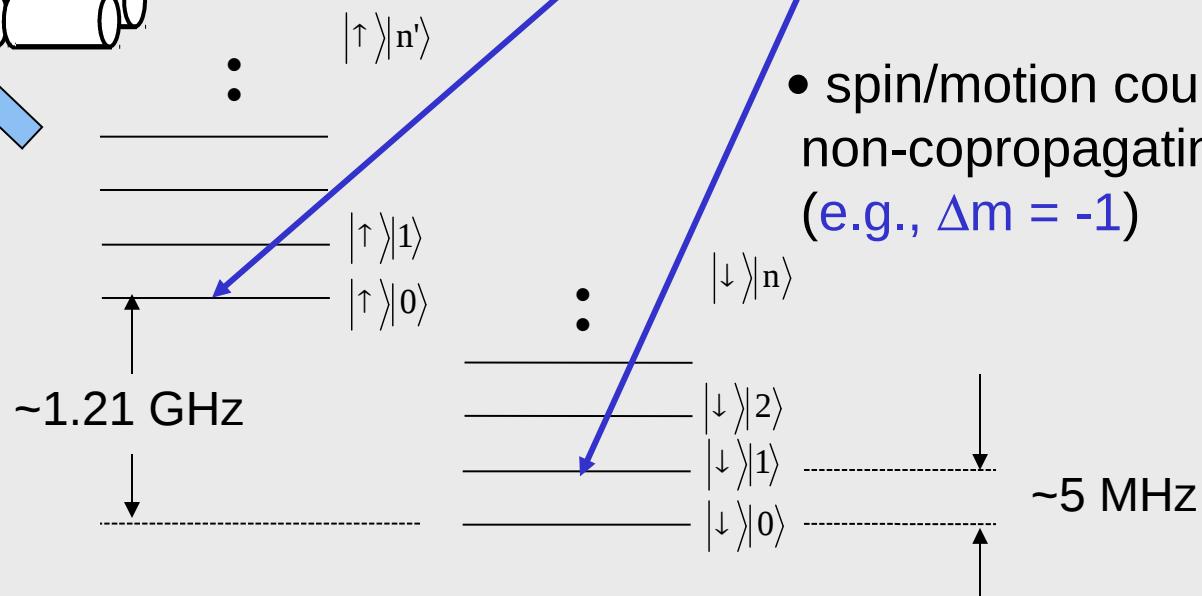
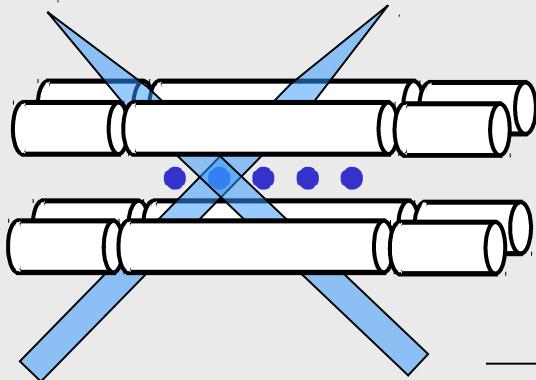
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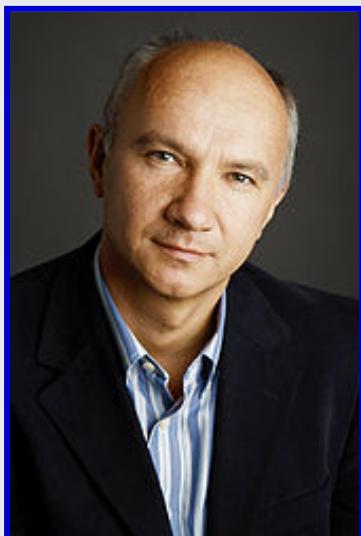
$B \approx 119$ G (coherence time ~ 10 s)



A bit more history:



Peter Shor: algorithm for efficient number factoring
on a quantum computer (~ 1994)

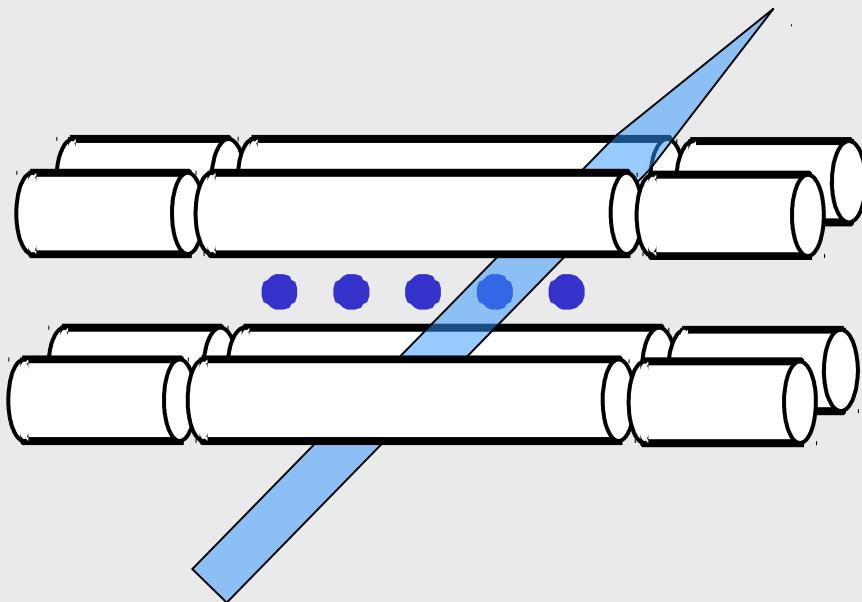


Artur Ekert: presentation at the 1994
International Conference on Atomic Physics
Boulder, Colorado

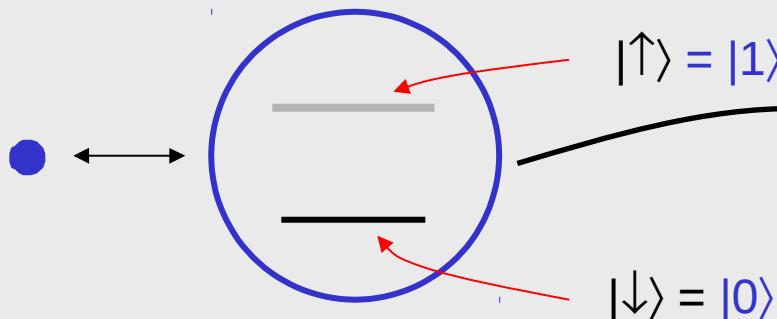
Atomic ion quantum computer:

J. I. Cirac, P. Zoller, Phys. Rev. Lett. **74**, 4091 (1995)

1. START MOTION IN GROUND STATE
2. SPIN → MOTION MAP



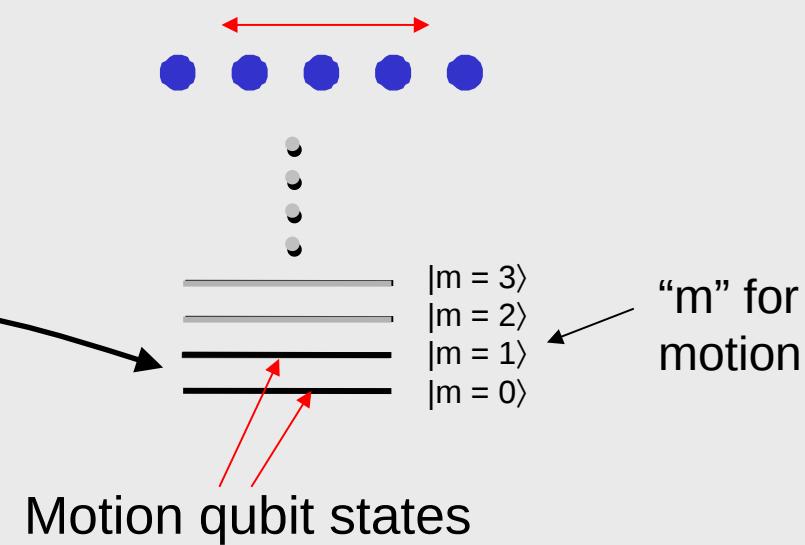
INTERNAL STATE “SPIN” QUBIT



Ignacio Cirac

Peter Zoller

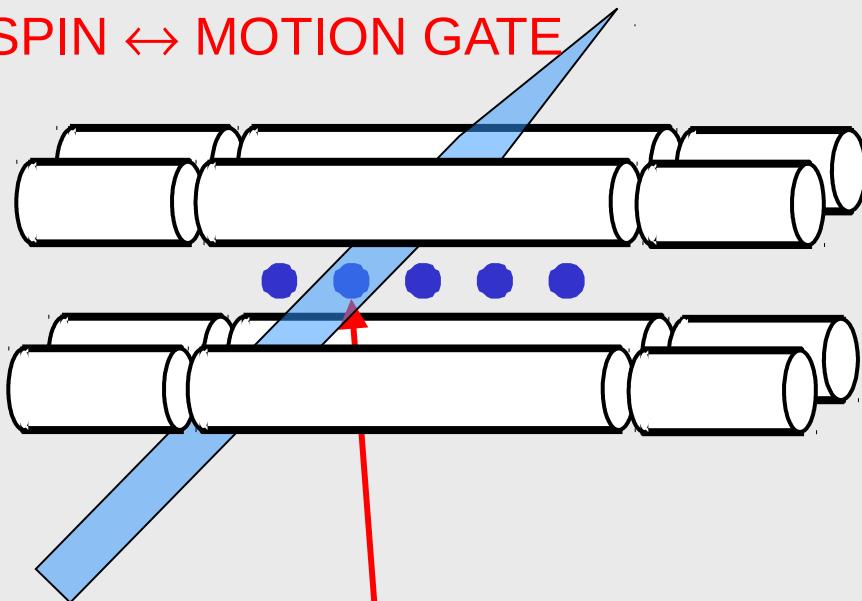
MOTION “DATA BUS”
(e.g., center-of-mass mode)



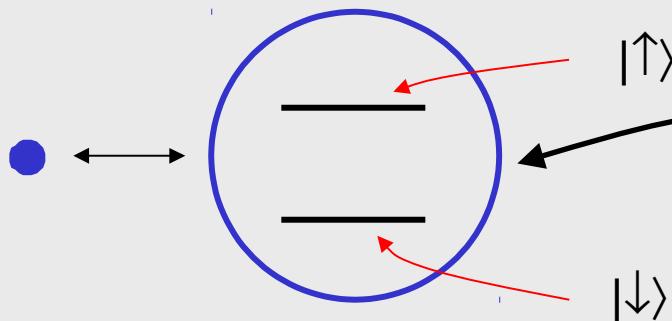
Atomic ion quantum computation:

J. I. Cirac, P. Zoller, Phys. Rev. Lett. **74**, 4091 (1995)

1. START MOTION IN GROUND STATE
2. SPIN \rightarrow MOTION MAP
3. SPIN \leftrightarrow MOTION GATE



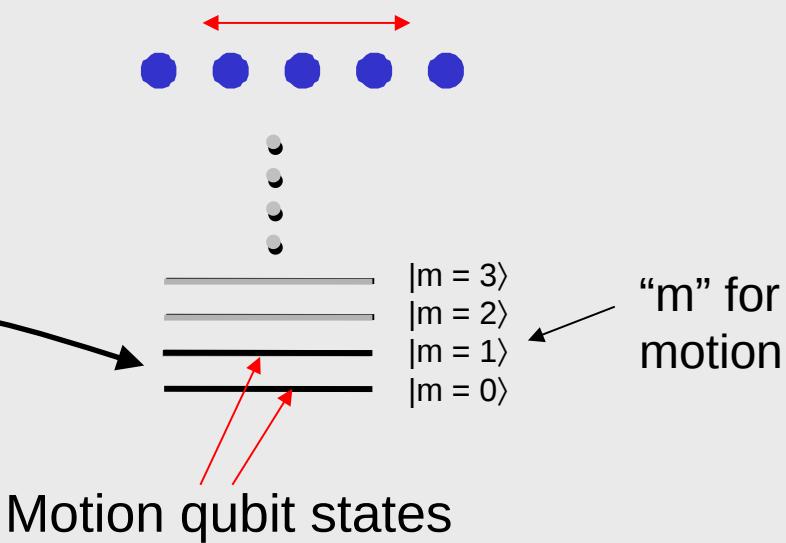
INTERNAL STATE “SPIN” QUBIT



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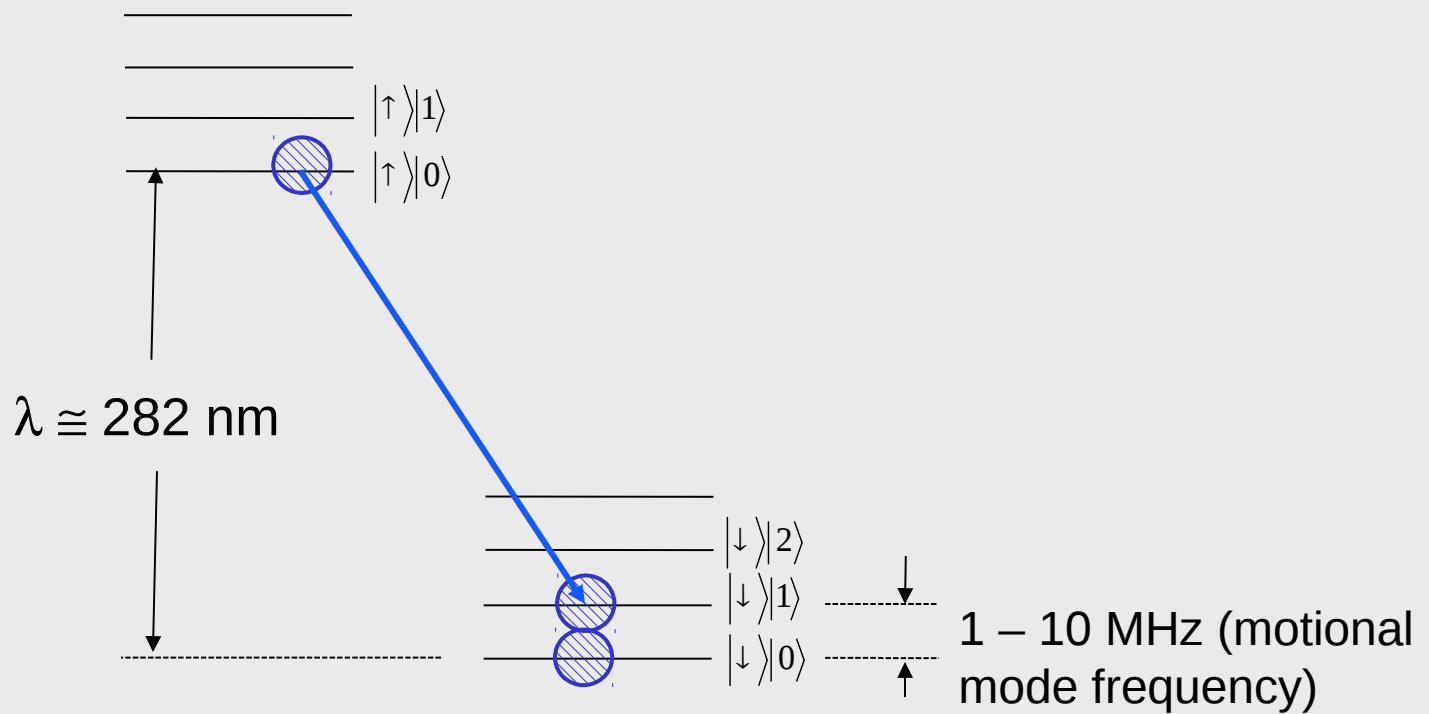
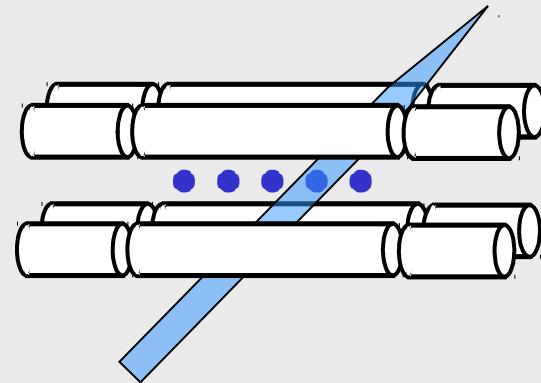
Peter Zoller

MOTION “DATA BUS”
(e.g., center-of-mass mode)



Step 2. Spin → motion map

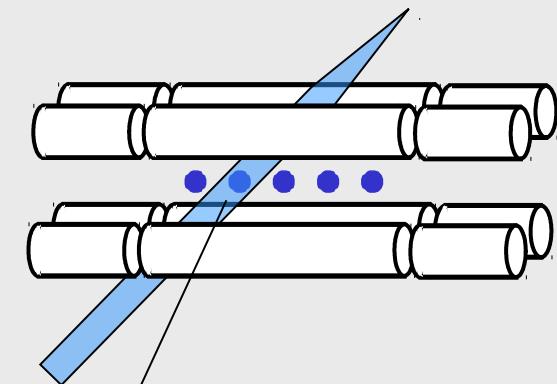
$$(\alpha|\downarrow\rangle + \beta|\uparrow\rangle)|0\rangle \rightarrow |\downarrow\rangle(\alpha|0\rangle + \beta|1\rangle)$$



Step 2: Spin-qubit/motion-qubit logic gate

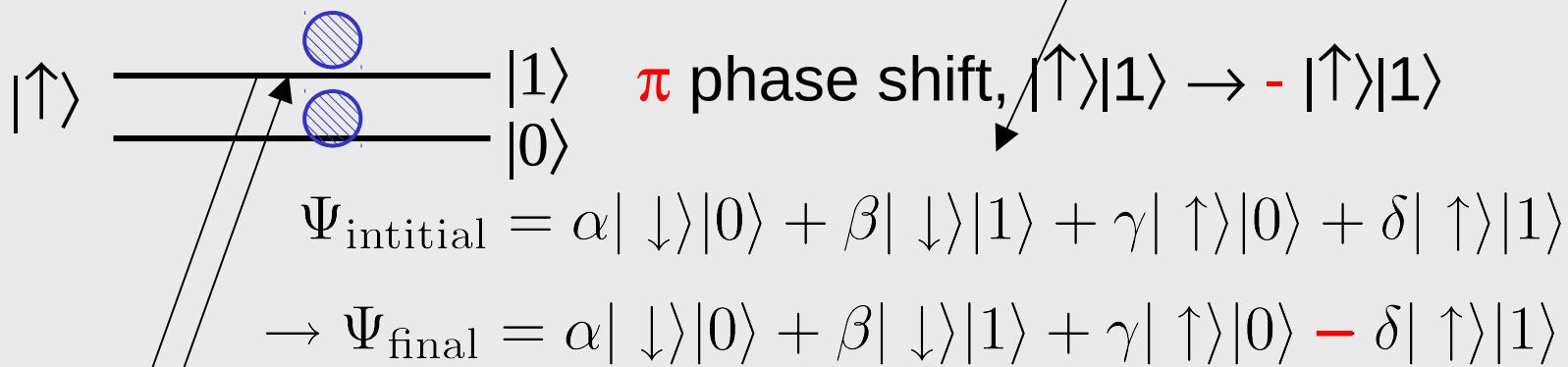
(Chris Monroe et al., Phys. Rev. Lett. **75**, 4714 (1995)).

Hyperfine states of ${}^9\text{Be}^+$ coupled with stimulated-Raman transitions

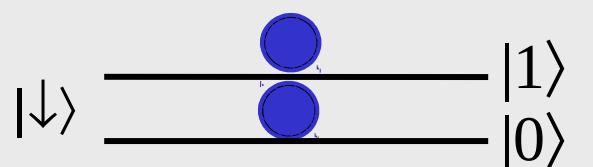
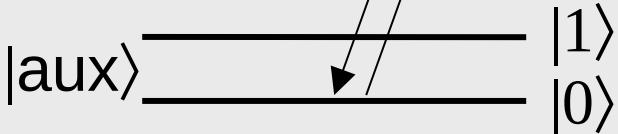


Complete Cirac-Zoller gate (two ions):

(F. Schmidt-Kaler et al., Nature, **422**, 408 (2003), Innsbruck)



Cirac – Zoller gates:
need precise control of motion quantum states.
Alternative gates suppress this problem.



“Motion-insensitive” gates (in Lamb-Dicke limit: wave function $\ll \lambda$)

K. Mølmer and A. Sørensen, Phys. Rev. Lett. **82**, 1835 (1999).

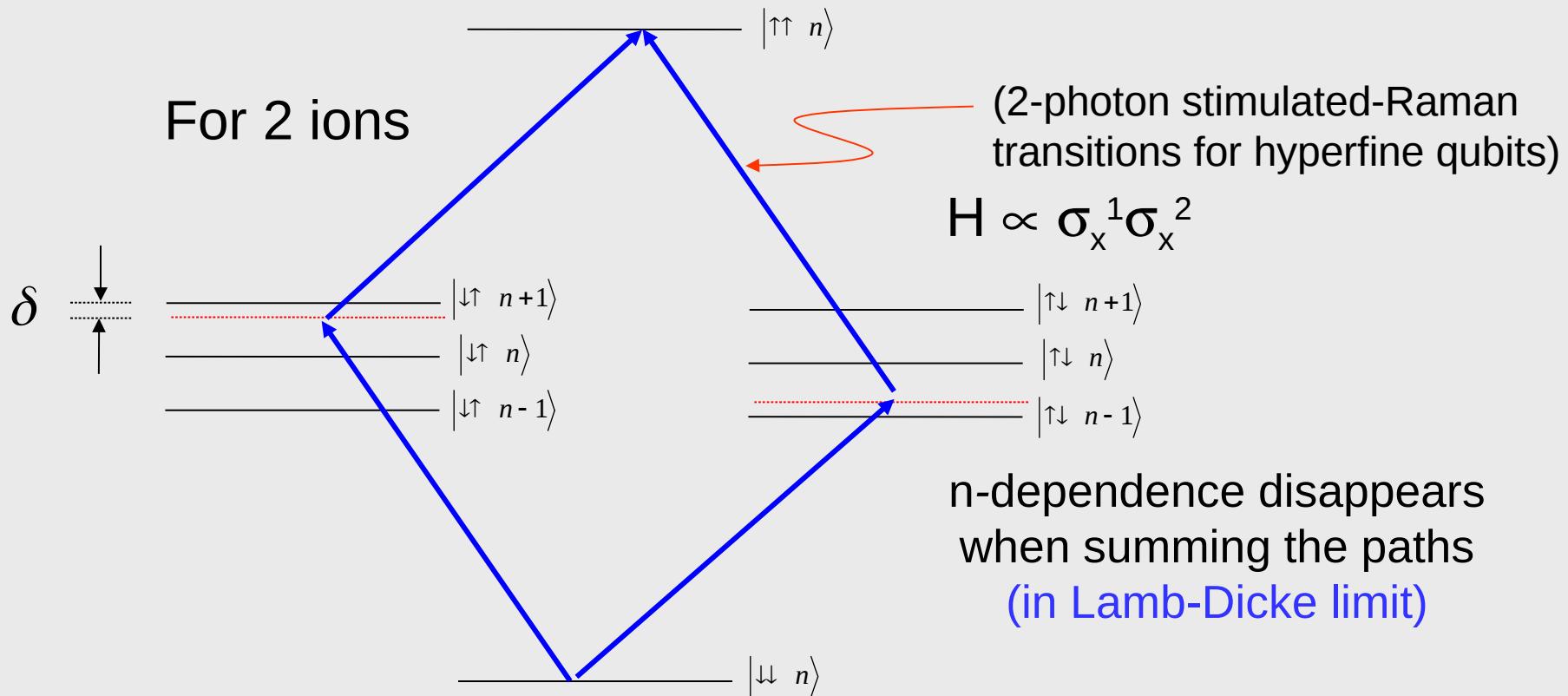
A. Sørensen and K. Mølmer, Phys. Rev. Lett. **82**, 1971 (1999).

E. Solano, R. L. de Matos Filho, and N. Zagury, Phys. Rev. A **59**, 2539 (1999).

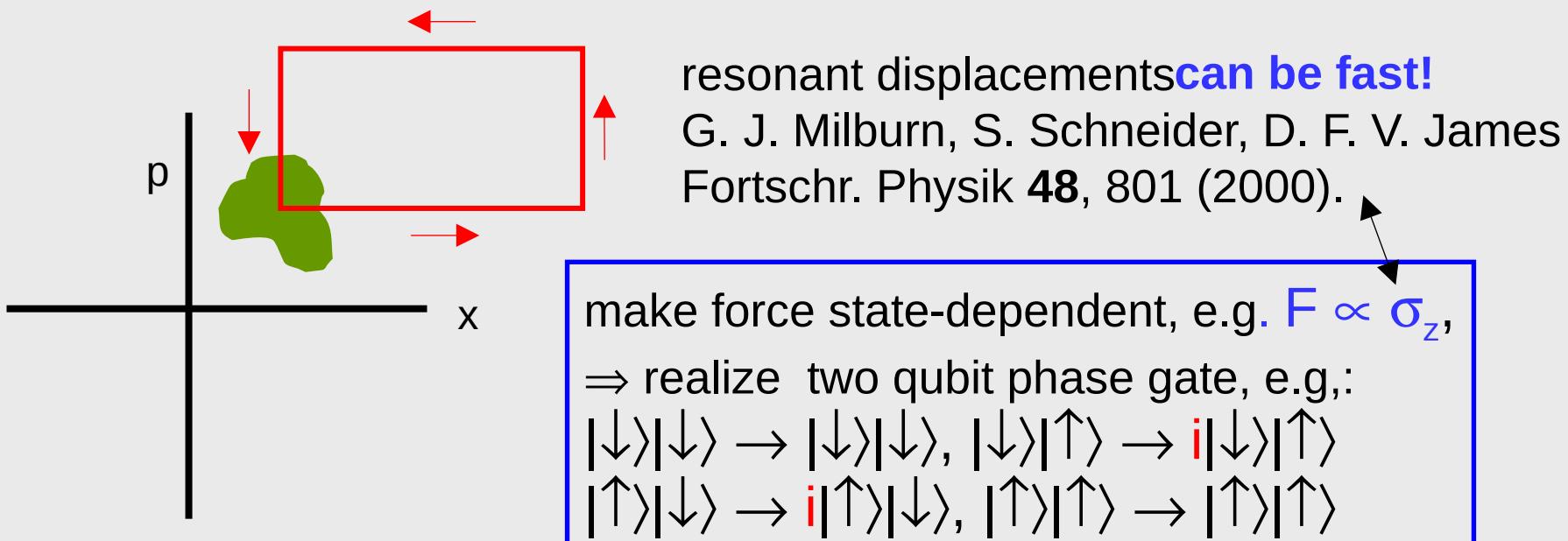
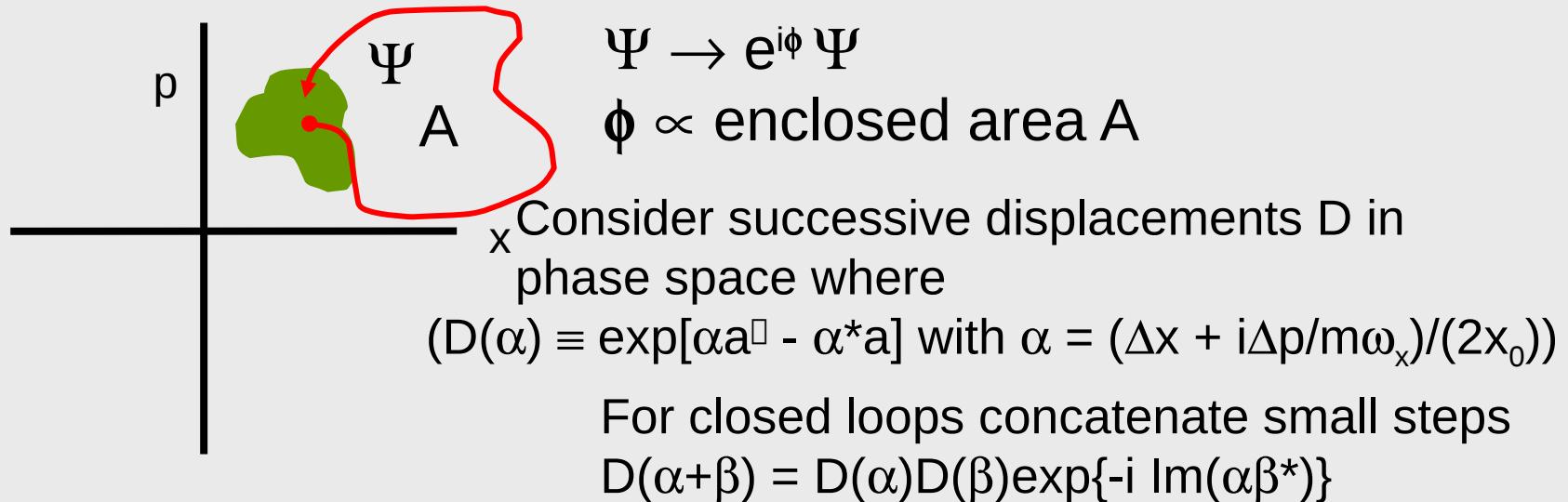
A. Sørensen and K. Mølmer, Phys. Rev. A **62**, 02231 (2000).

G. J. Milburn, S. Schneider, and D. F. V. James, Fortschr. Physik **48**, 801 (2000).

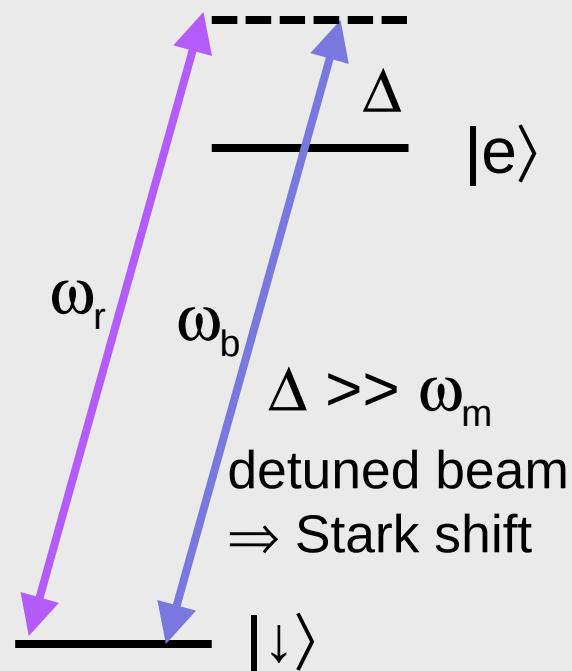
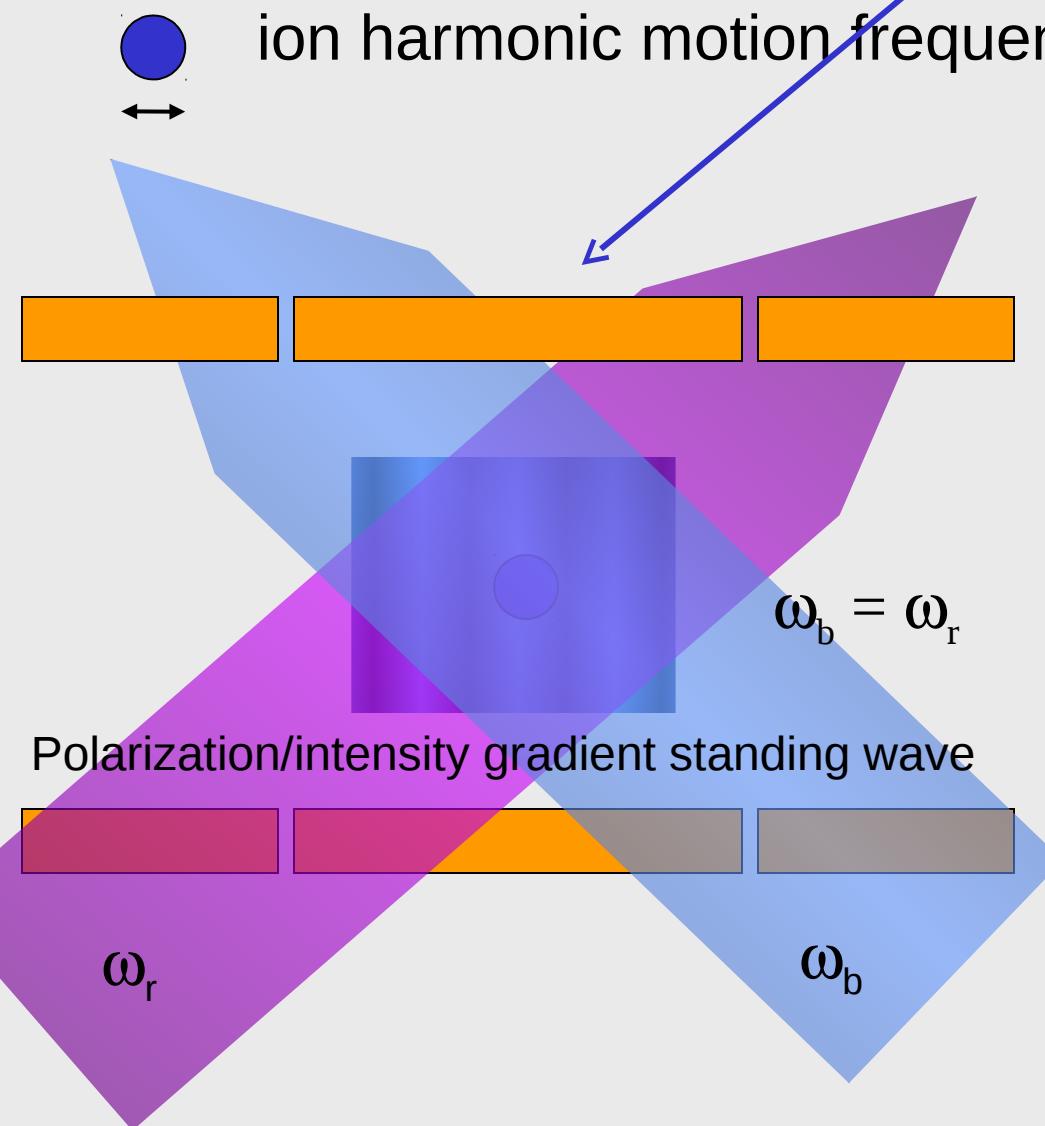
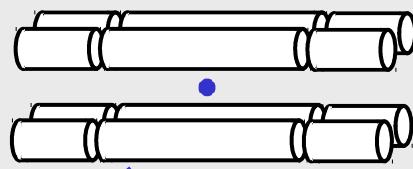
X. Wang, A. Sørensen, and K. Mølmer, Phys. Rev. Lett. **86**, 3907 (2001).



Can view gates in terms of geometric phases:
phase-space diagram for selected motional mode:

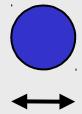


optical dipole forces for phase-space displacements

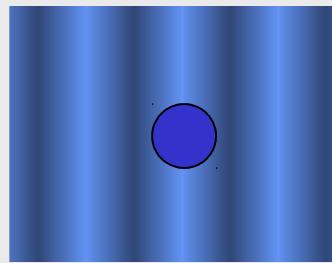


basic idea: use
gradient of Stark shift
to apply force

Dipole forces to displace ions in phase space



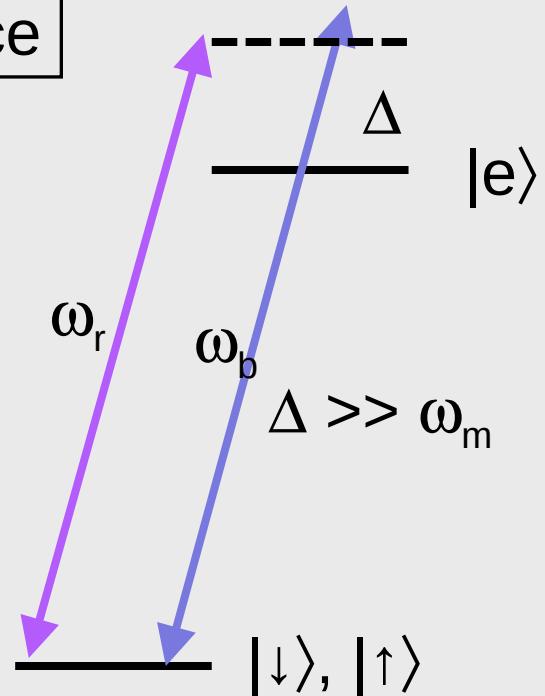
ion harmonic motion frequency ω_m



“walking” standing wave

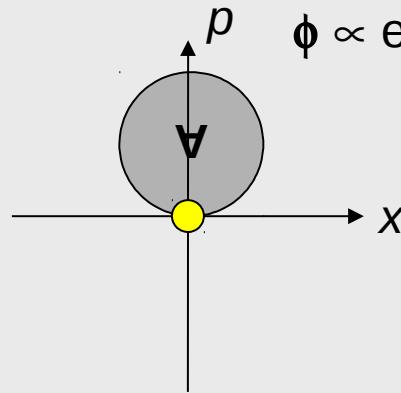


$$\omega_b = \omega_r + \omega_m + \delta$$



$$\Psi \rightarrow e^{i\phi} \Psi$$

$\phi \propto$ enclosed area A



2-ion phase-gate example (e.g., stretch mode, $F_{\uparrow} = -F_{\downarrow}$ (i.e., $F \propto \sigma_z$))

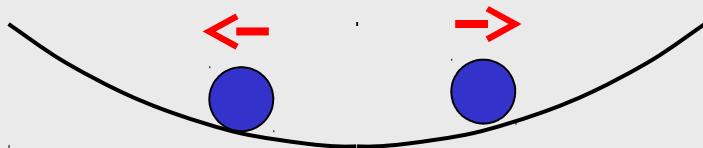
$$\omega_b - \omega_a = \omega_{\text{stretch}} + \delta$$

apply forces for $t = 2\pi/\delta$

\uparrow
 p

$$\Psi \rightarrow e^{i\phi} \Psi$$

$\phi \propto \text{enclosed area } A$

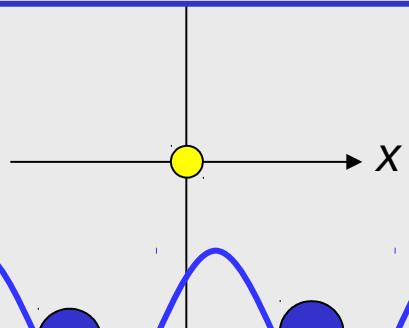


Strengths:

- individual ion addressing not required
- Doesn't depend on initial motion wave function, but we want:
 - spread of wave function $\ll \lambda_{\text{eff}}$
 - amplitude of excitation $\ll \lambda_{\text{eff}}$
- Same picture for $\sigma_{z1}\sigma_{z2}$ and $\sigma_{x1}\sigma_{x2}$ gates (just different basis states)
(P. J. Lee et al., J. Opt. B: Quantum Semiclass. Opt. 7, S371 (2005))

Lamb-Dicke regime

$|\downarrow\rangle|\downarrow\rangle$:



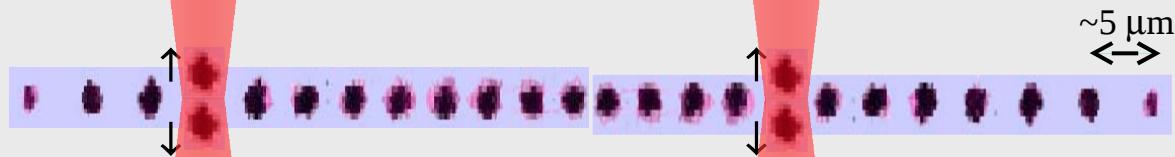
$$|\downarrow\rangle|\downarrow\rangle \rightarrow |\downarrow\rangle|\downarrow\rangle$$

$$|\uparrow\rangle|\uparrow\rangle \rightarrow |\uparrow\rangle|\uparrow\rangle$$



Apply gate to selected ions in linear array

(Chris Monroe group, U. Md.
and Rainer Blatt group, Innsbruck)



$$G = e^{-i\sigma_x^{(1)}\sigma_x^{(2)}\varphi}$$

Ising interaction

Simulation

$$H = \sum_{i < j} J_{i,j} \hat{\sigma}_z^{(i)} \hat{\sigma}_z^{(j)} + B \sum_i \hat{\sigma}_y^{(i)} \quad \text{etc.}$$



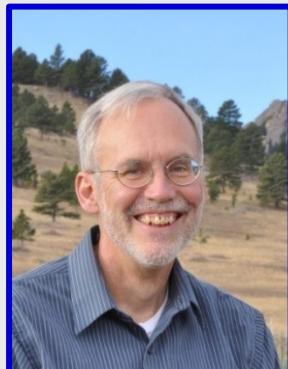
Chris Monroe

JQI, Maryland
e.g., P. Richerme et al.,
Nature **511**, 198 (2014)

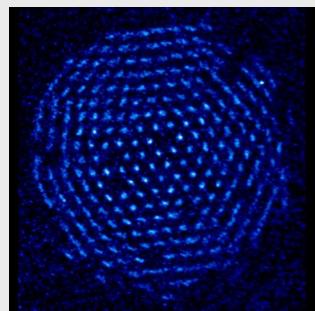


Rainer Blatt

Innsbruck
e.g., P. Jurcevic et al.,
Nature **511**, 202 (2014)



John Bollinger

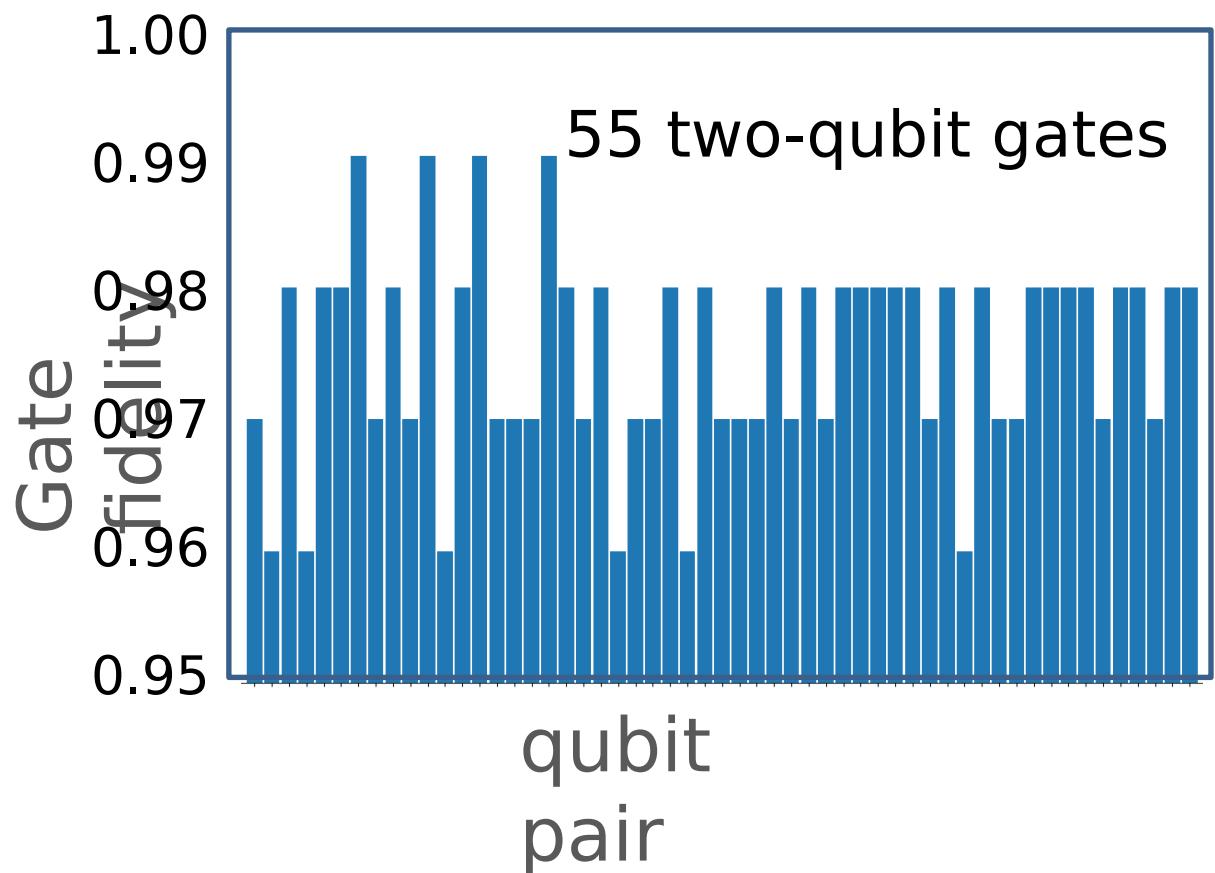
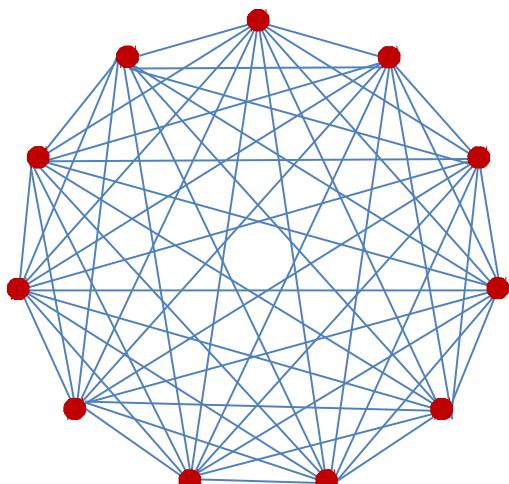


2D Wigner crystal

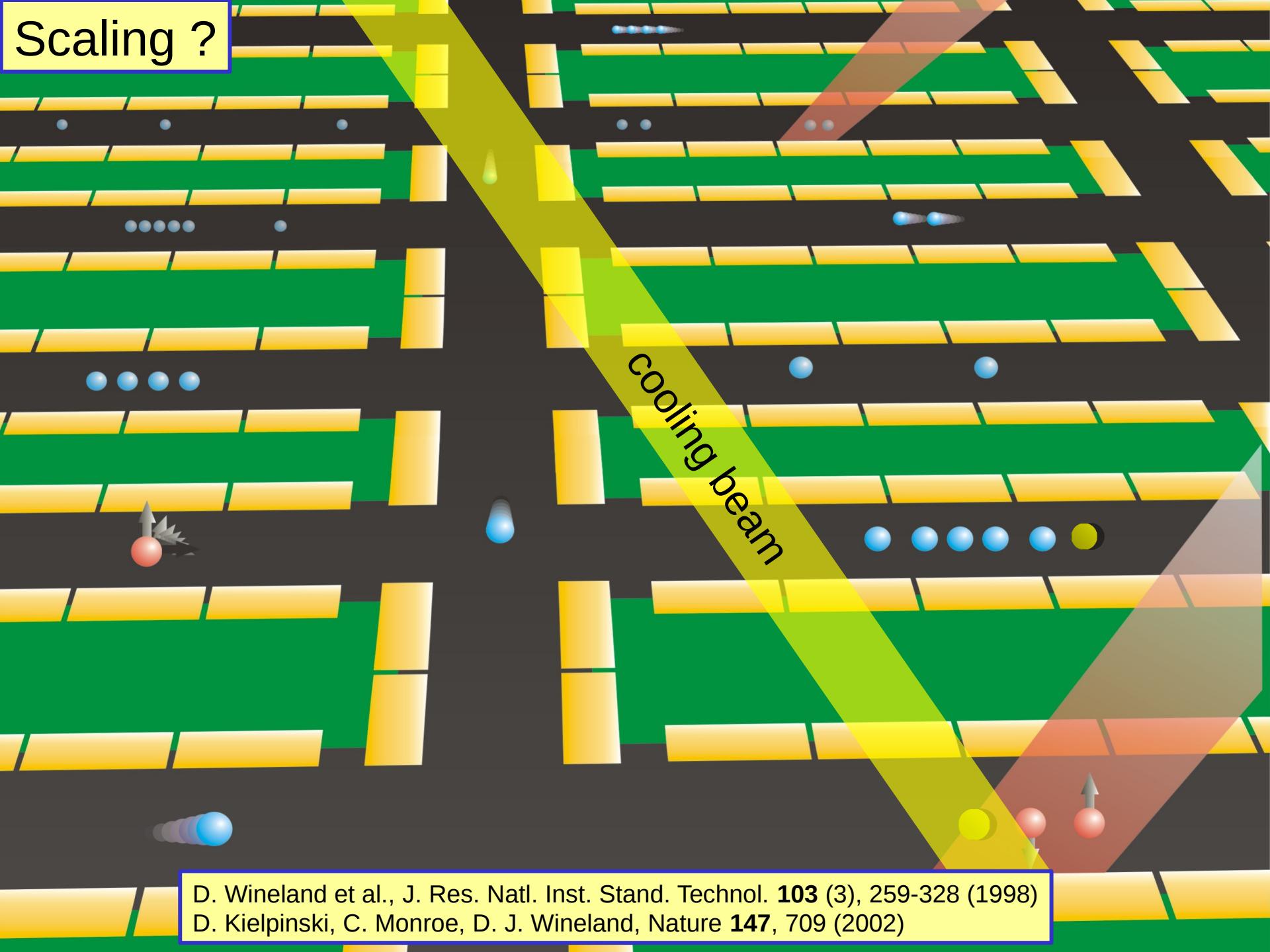
NIST
e.g., J. G. Bohnet et al.,
Sci. **352**, 1297 (2016)

“Full connectivity” (11 qubits)

K. Wright et al., arXiv:1903.08181

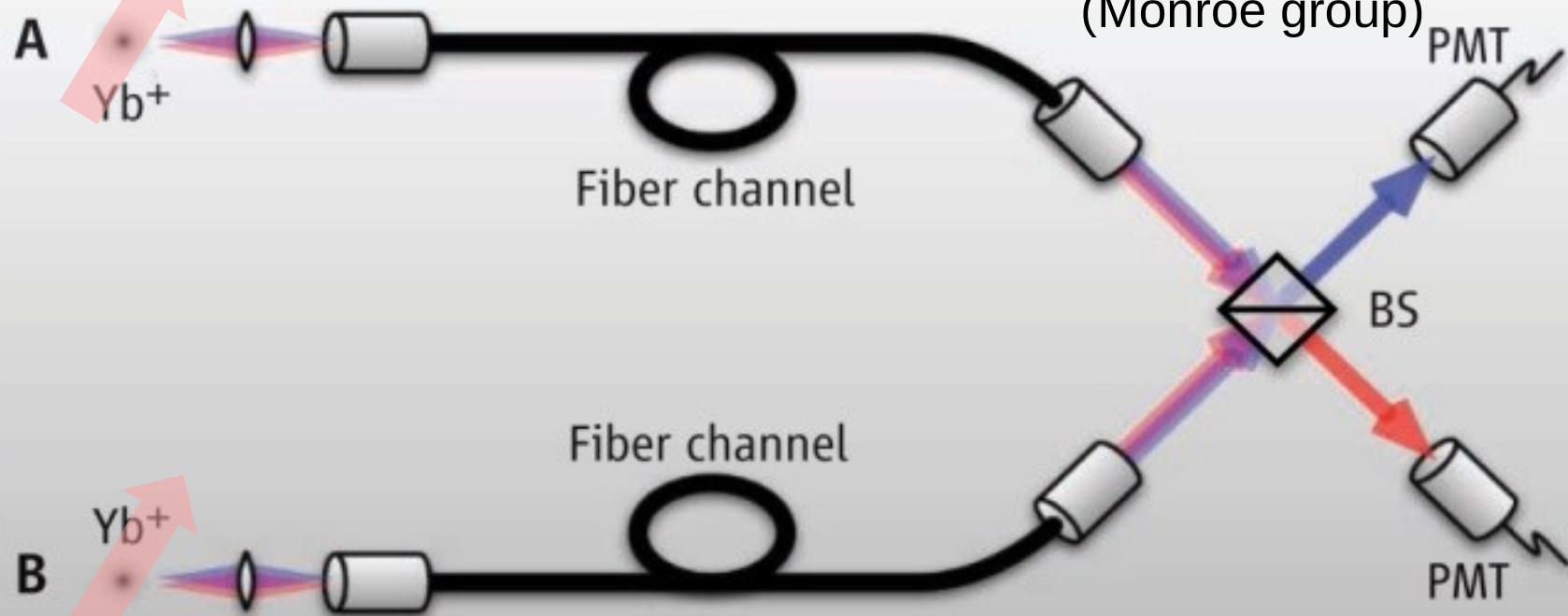


Scaling ?



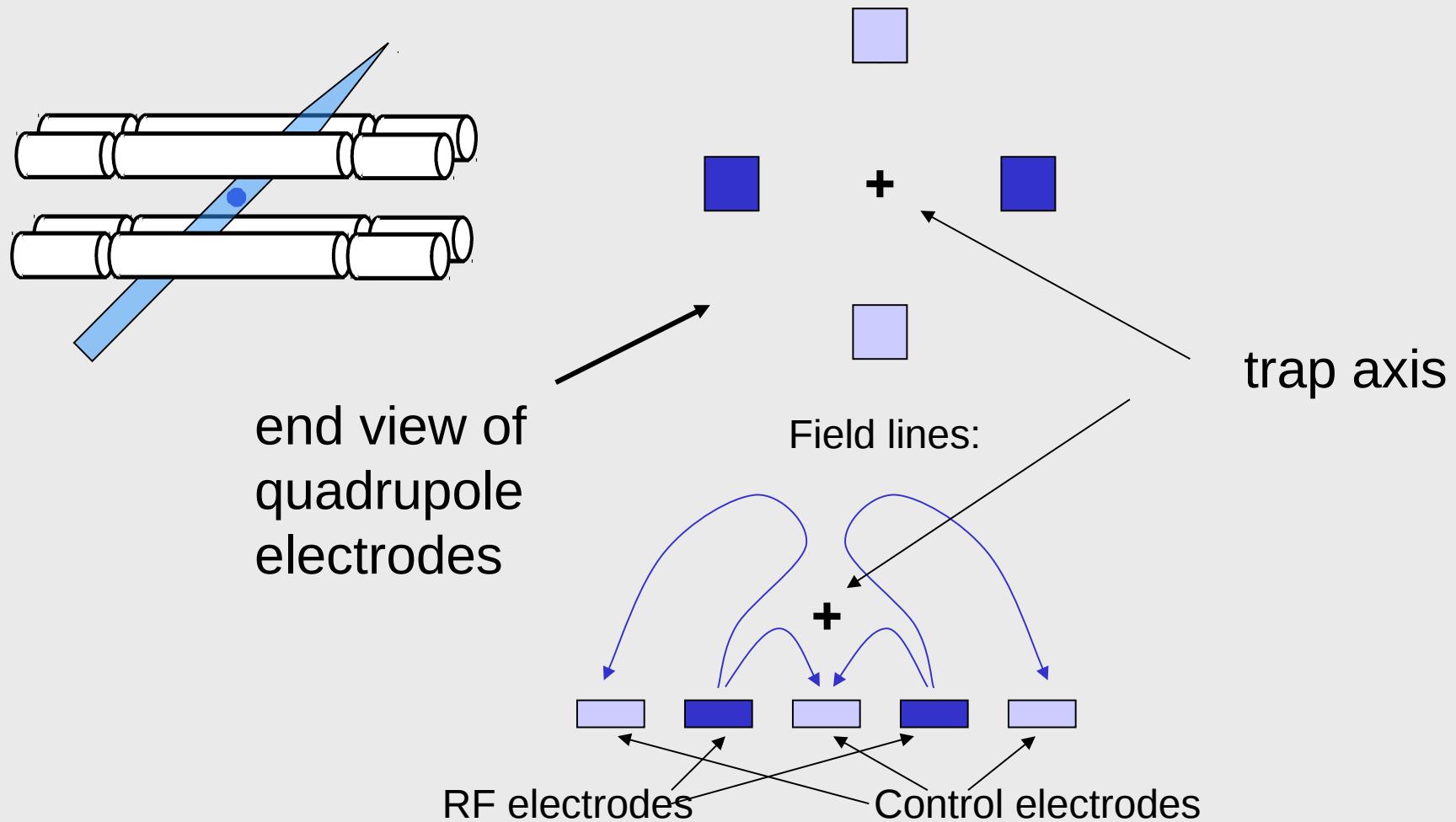
D. Wineland et al., J. Res. Natl. Inst. Stand. Technol. **103** (3), 259-328 (1998)
D. Kielpinski, C. Monroe, D. J. Wineland, Nature **147**, 709 (2002)

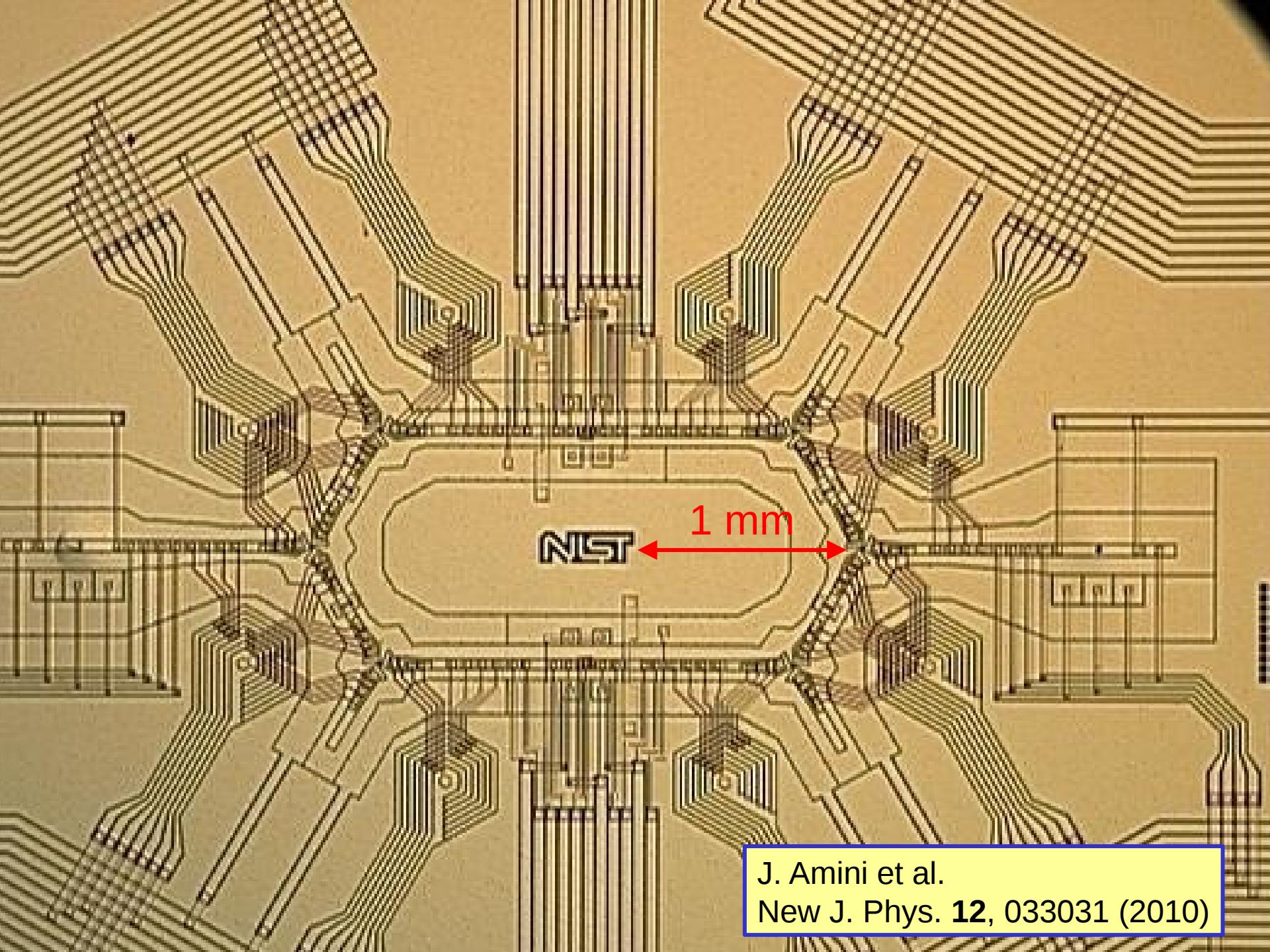
Or, entangle remote ions via ion/photon entanglement
(Monroe group)



- teleport qubits and logic gates between sites in quantum processor
 - connect nodes in quantum communication network
- C. Monroe and J. Kim, *Science* **339**, 1164 (2013)

Surface-electrode traps





J. Amini et al.
New J. Phys. **12**, 033031 (2010)

Atomic ion experimental groups pursuing quantum information & metrology

Aarhus
AFRL-Rome
Amherst
ARL-Adelphi
Basel
Berkeley
Bonn
Buenos Aires
CERN
Croatia
Delft
Dresden
Edinburgh
Erlangen
Fribourg
Georgia Tech
GTRI
Griffith
Hannover
Honeywell
Imperial (London)
Indiana
Innsbruck
IonQ
Lincoln Labs
Marseille
MIT
Munich/Garching
NIST, Boulder
Northwestern
NPL
Osaka
Oxford
Paris (Université Paris)

+ many other platforms:
neutral atoms, Josephson junctions,
quantum dots, NV centers in diamond,
single photons, ...

Freiburg
Georgia Tech
GTRI
Griffith
Hannover
Honeywell
Imperial (London)
Indiana
Innsbruck
IonQ
Lincoln Labs
Marseille
Singapore
SK Telecom, S. Korea
Sussex
Sydney
Tsinghua (Beijing)
UCLA
U. Oregon
U. Washington
Waterloo
Weizmann Institute
Williams

Future?

- Computers
 - ◊ “More and better” (more qubits, smaller gate errors)
2 qubit gate errors $\sim 10^{-3}$, want $< 10^{-4}$
 - ◊ problem areas: e.g., for ions – “anomalous heating”
 - ◊ need error correction!
- Factoring machine?
- Simulation
 - ◊ mimic the dynamics of another quantum system of interest
- Metrology
 - ◊ “quantum-logic” spectroscopy
 - ◊ improve beyond standard quantum limit for phase measurements
- Commercial: D-wave, IBM, Google, Microsoft, Rigetti Computing, Quantum Circuits, IonQ, AQT, ... (quantumcomputingreport.com)
- ???

COMMERCIAL INTEREST (IONS)

Honeywell

honeywell.com/quantumsolutions

STARTUPS



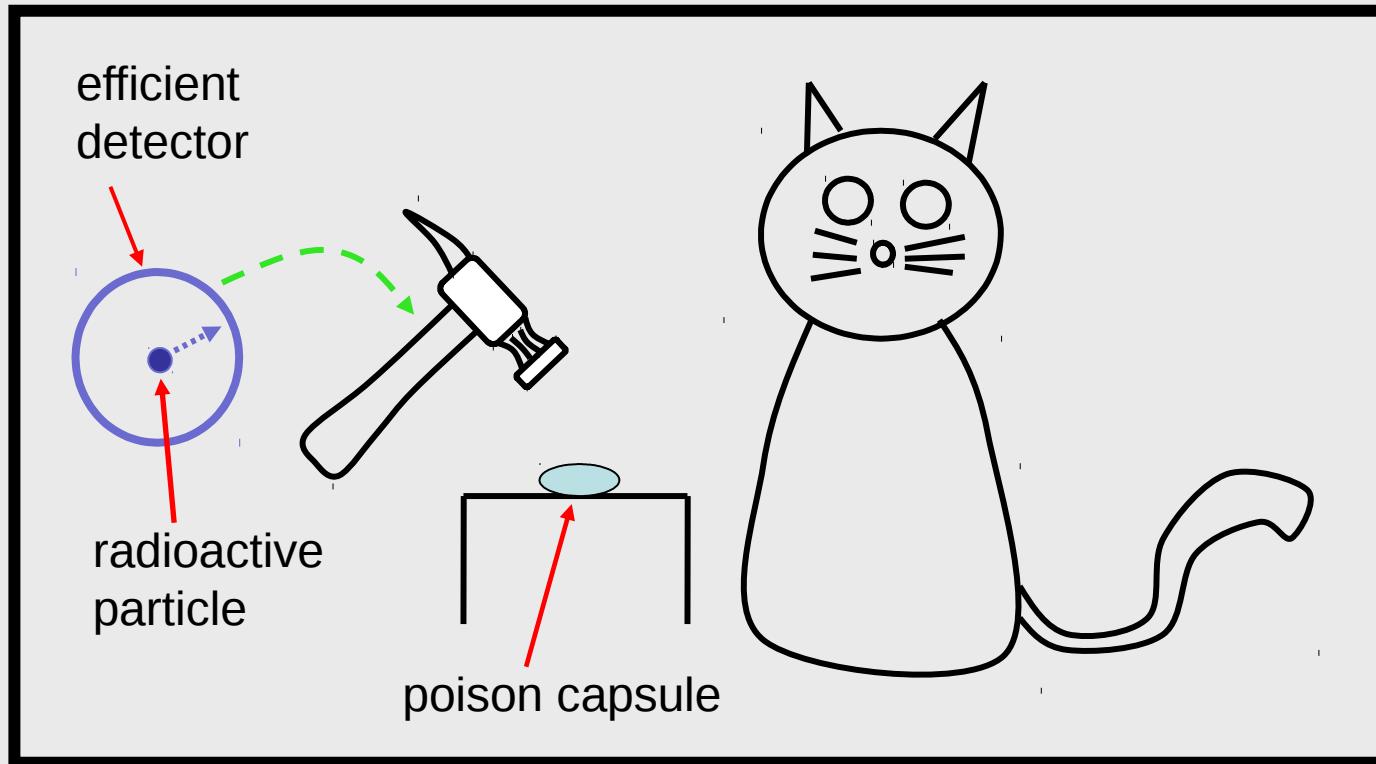
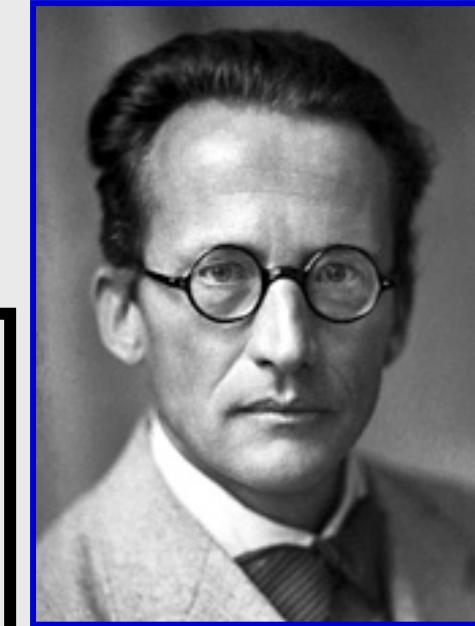
ionq.co (C. Monroe, J. Kim, ...)



Alpine Quantum Technologies, aqt.eu
(R. Blatt, P. Zoller, T. Monz...)

Erwin Schrödinger's Cat (1935)

(extrapolating ideas of quantum mechanics
from microscopic to macroscopic world)

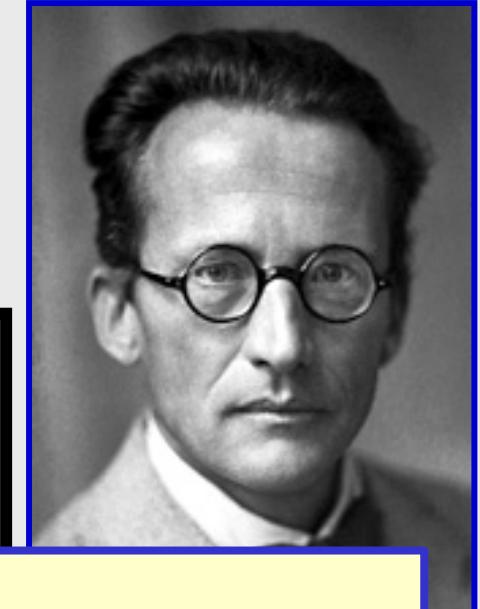


At “half-life” of particle, quantum mechanics says
cat is simultaneously dead and alive!

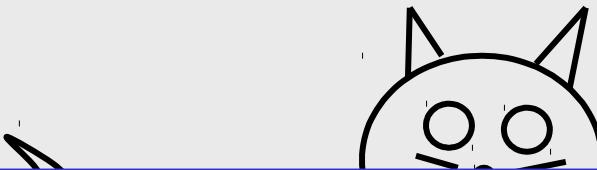
“entangled” superposition $\Psi = |\text{alive}\rangle|\text{dead}\rangle + |\text{dead}\rangle|\text{alive}\rangle$

Erwin Schrödinger's Cat (1935)

(extrapolating ideas of quantum mechanics
from microscopic to macroscopic world)



efficient
detector



Schrödinger (1952):

“We never experiment with just one electron or atom or (small) molecule. In thought experiments, we sometimes assume that we do; this invariably entails ridiculous consequences...”

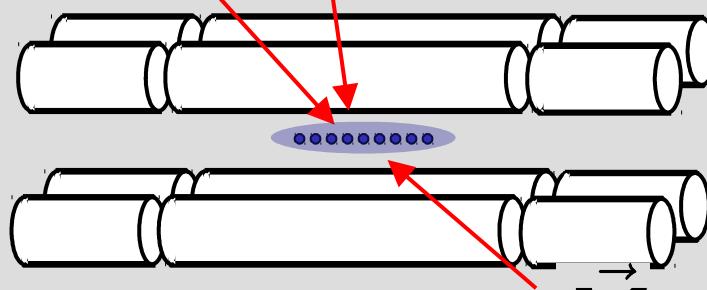
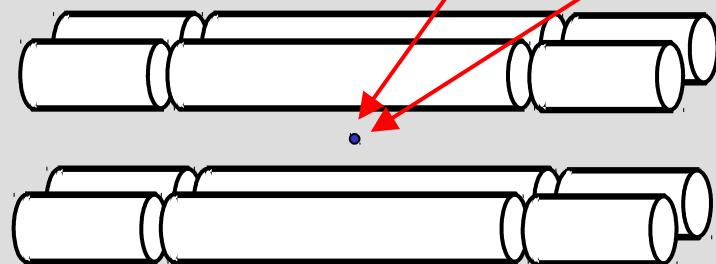
At “half-life” of particle, quantum mechanics says
cat is simultaneously dead and alive!

“entangled” superposition $\Psi = |\bullet\rangle|\text{alive}\rangle + |\circlearrowleft\rangle|\text{dead}\rangle$

Special superposition state made with quantum computer: Schrödinger's cat?

$$\Psi(t) = |0\rangle_1 |0\rangle \dots = |\bullet\circlearrowleft\rangle |\bullet\circlearrowright\rangle + |\circlearrowleft\bullet\rangle |\circlearrowright\bullet\rangle \dots |1\rangle_N$$

For large N $\Psi = |0\rangle_1 \vec{M}_\downarrow + |1\rangle_1 \vec{M}_\uparrow$



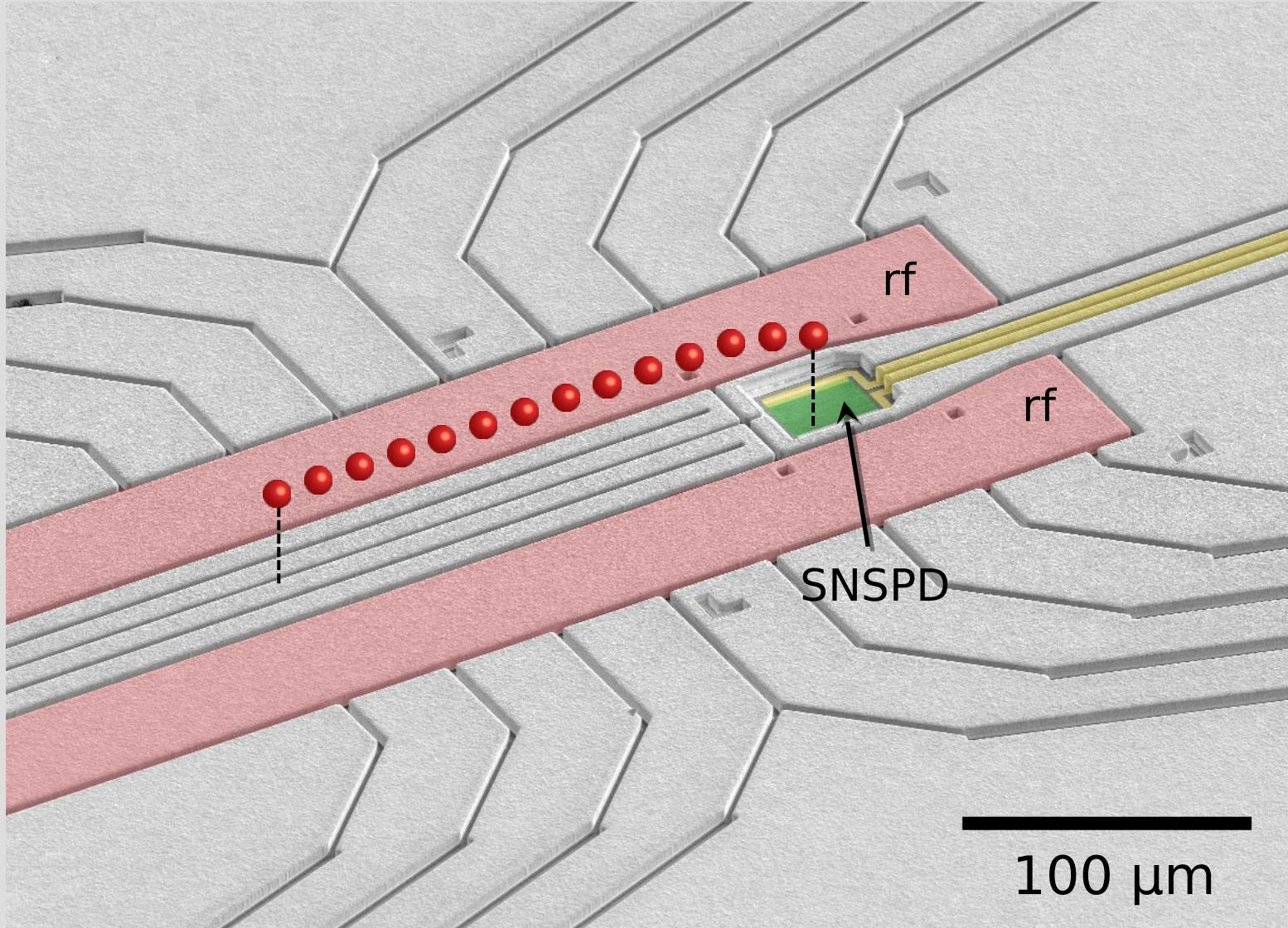
Classical
meter

\vec{M}
macroscopic
magnetization

NIST IONS, December 2018

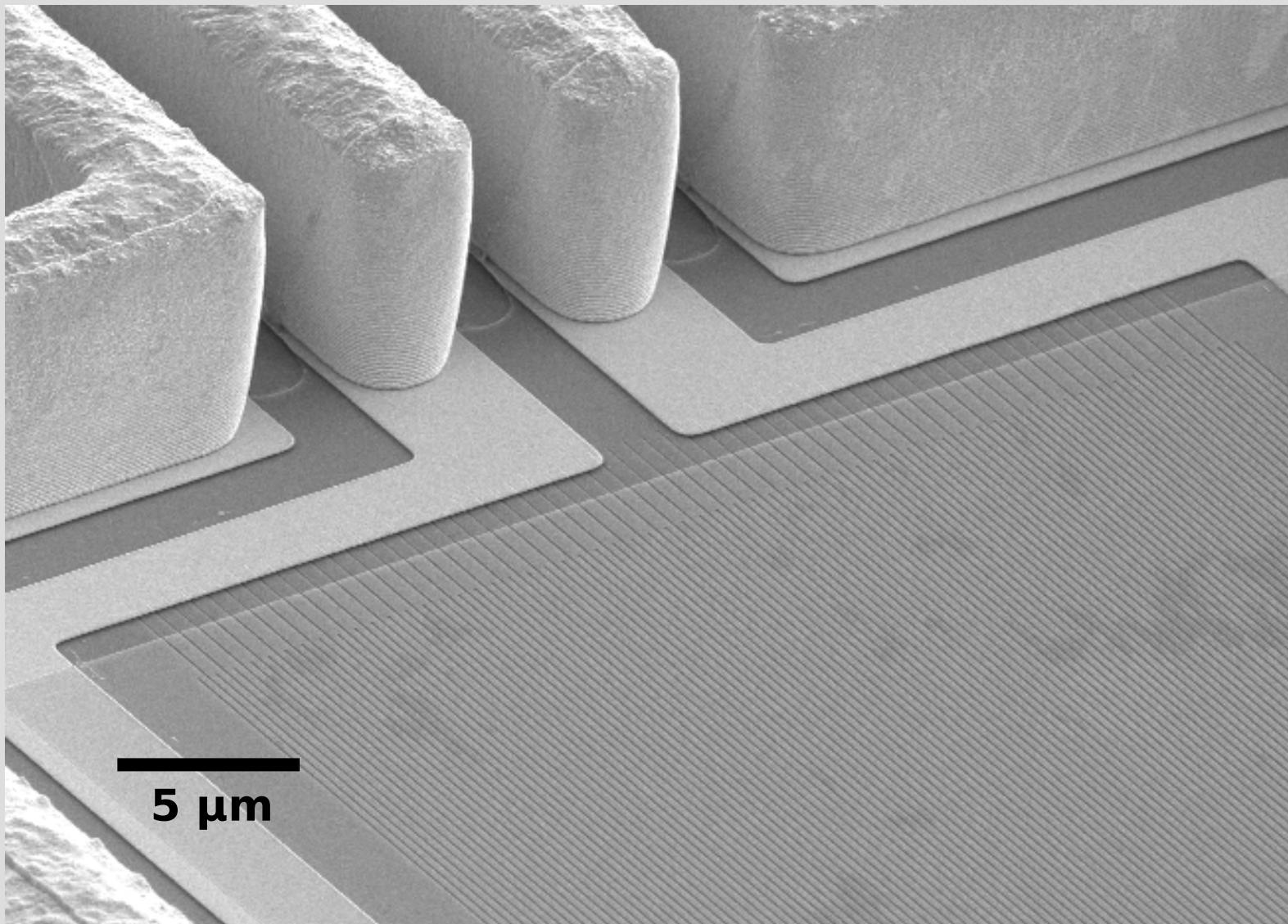


Linear RF trap with integrated SNSPD (D. Slichter et al., NIST)



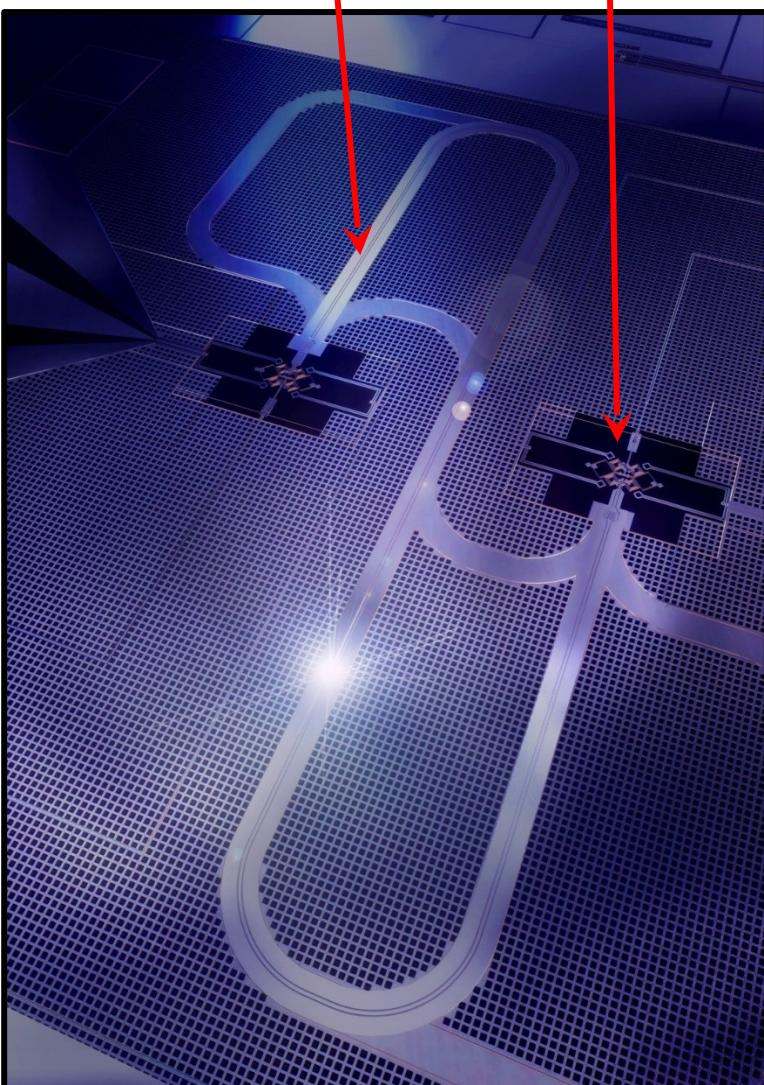
Detector NA =
0.24(2)

Superconducting nanowire meander (MoSi)



Superconducting qubits

e.g., Josephson-junction qubits
coupled with stripline cavities



UCSB/Google – J. Martinis
Yale – M. Devoret, R. Schoelkopf
UC Berkeley – I. Siddiqi, J. Clarke

IBM

BBN

CEA Saclay

Ecole Normale Supérieure – B. Huard

U Chicago – D. Schuster, A. Cleland

Princeton – A. Houck

NIST – R. Simmonds, J. Aumentado, J. Teufel, D. Pappas

IQC (Waterloo) – A. Lupascu, C. Wilson, M. Mariantoni

Colorado – K. Lehnert

Wisconsin – R. McDermott

Syracuse – B. Plourde

Washington U. in St. Louis – K. Murch

Tata Institute – R. Vijay

U Pittsburgh – M. Hatridge

Kansas – S. Han

MIT/Lincoln Labs – W. Oliver, T. Orlando

Delft – L. DiCarlo, H. Mooij

ETH Zurich – A. Wallraff

U Grenoble – O. Buisson

U Tokyo – Y. Nakamura

NEC – J. Tsai

NTT – K. Semba

Royal Holloway – O. Astafiev

Maryland/JQI – F. Wellstood, K. Osborn,
B. Palmer, V. Manucharyan

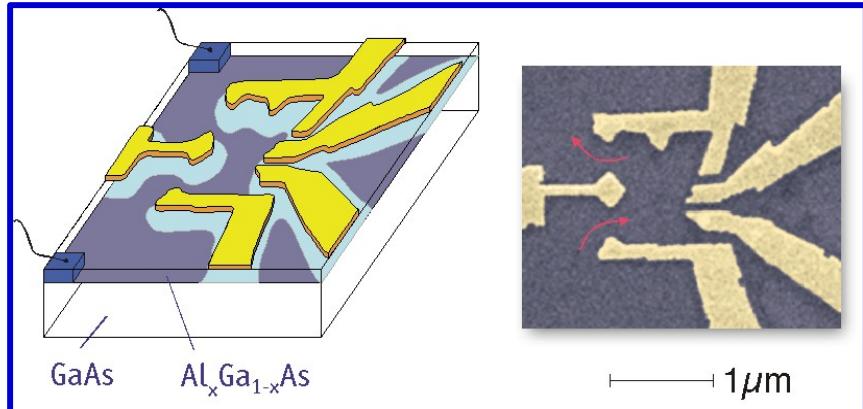
Innsbruck – G. Kirchmair

Chalmers – P. Delsing

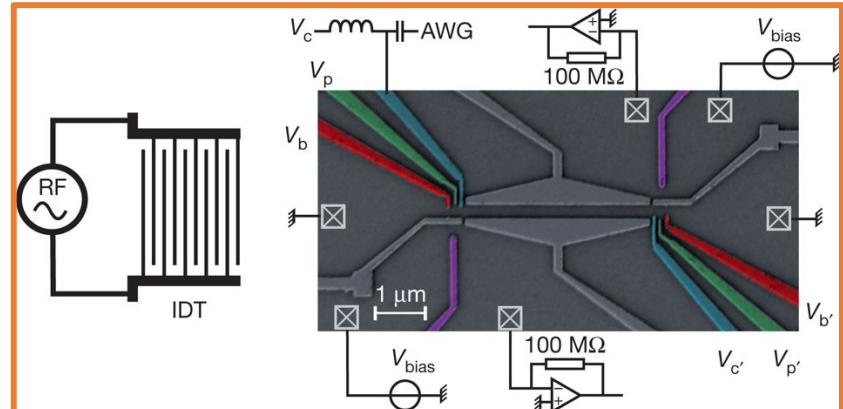
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Quantum dots/NV centers/SiC centers/P donors in Si

e.g., 2DEG GaAs Qubits



C. Marcus et al.



S. Hermelin et al., Nature **447**, 435 (2011)

HRL

Niels Bohr Institute – C. Marcus ...
U. Chicago – D. Awschalom...
Oxford – J. Morton...
U. New South Wales – A. Morello,
A. Dzurak, M. Simmons, S. Rogge
U. Sydney – D. Reilly ...
OIST (Okinawa) – Y. Kubo ...
ETH Zurich – K. Ensslin, A. Imamoglu
Harvard – M. Lukin,
A. Yacoby, R. Walsworth
UCSB – A. Gossard ...
MIT – D. Englund ...

NRC, Canada, A. Sachrajda ...

Princeton – J. Petta, S. Lyon, J. Thompson ...
Stanford – Y. Yamamoto, J. Vukovic ...
IQC (Waterloo) – M. Bajcsy ...
McGill – L. Childress ...
UC Berkeley – E. Yablonovitch, J. Bokor ...
LBNL – T. Schenkel ...
UCLA – H. Jiang ...
Delft – L. Kouwenhoven,
L. Vandersypen, R. Hanson ...
Wisconsin – M. Eriksson ...
TU-Munich – G. Abstreiter ...
Dortmund – M. Bayer ...
• • • • •