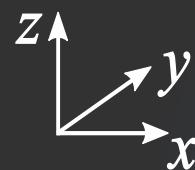
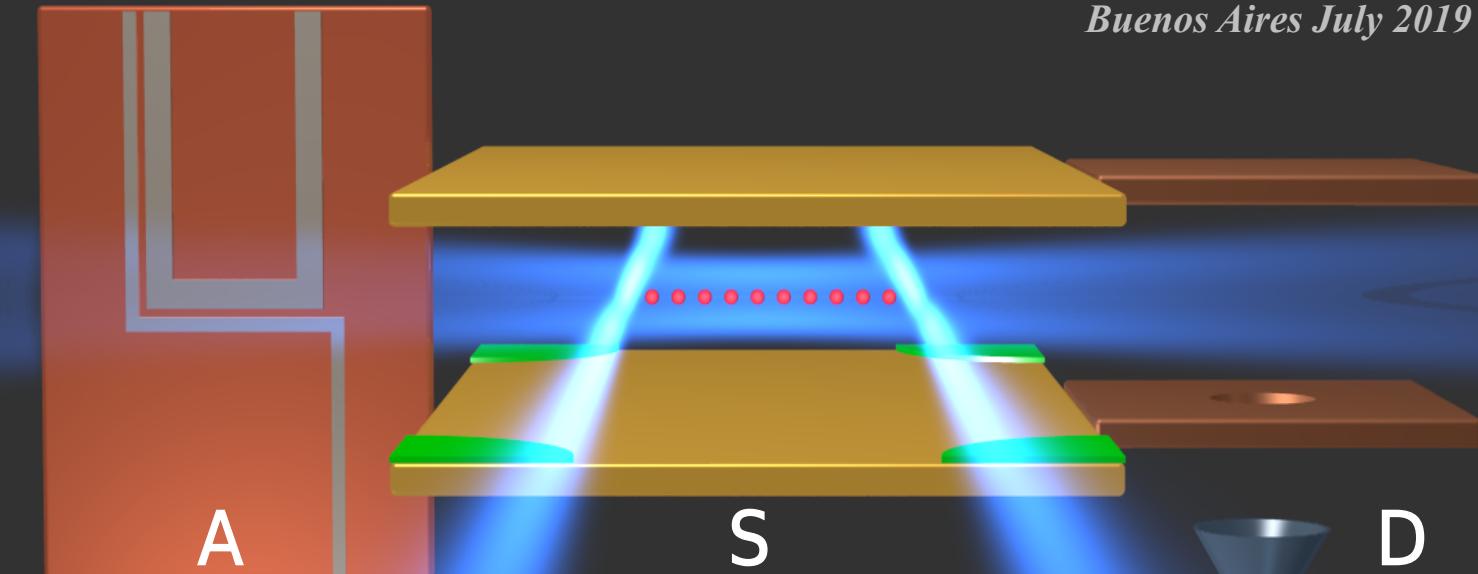




TRENSCRYBE



From cavity QED to quantum simulations with Rydberg atoms

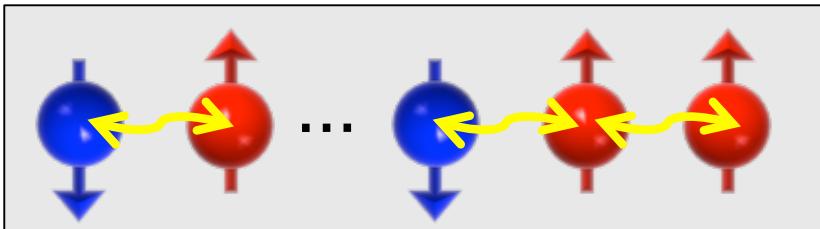
Lecture 3

Michel Brune



École Normale Supérieure, CNRS,
Université Pierre et Marie Curie,
Collège de France, Paris

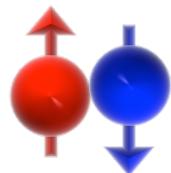
Spin chain quantum simulation



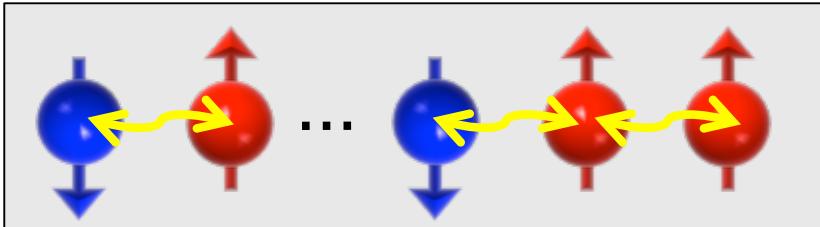
Simulation of a chain of interacting spins-1/2

Requirements?

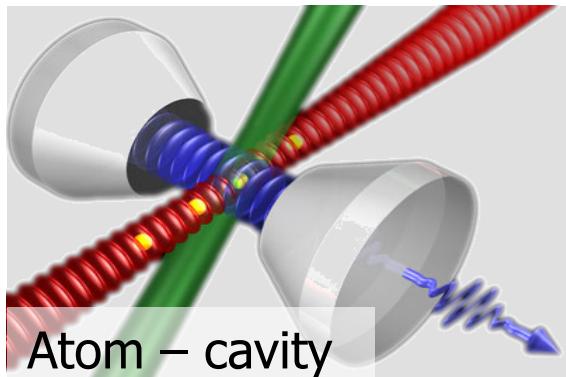
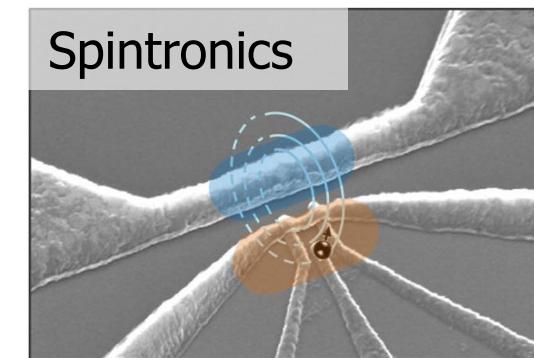
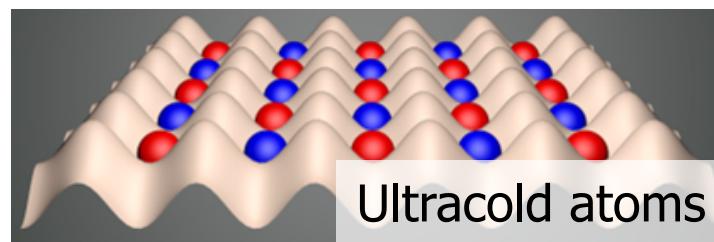
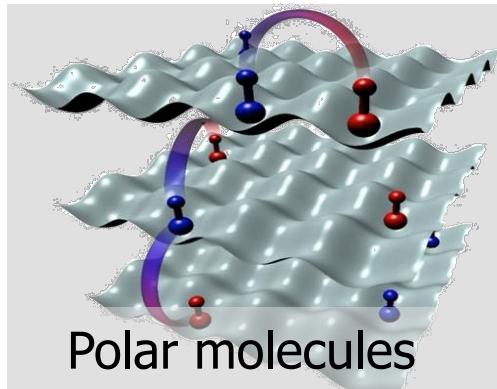
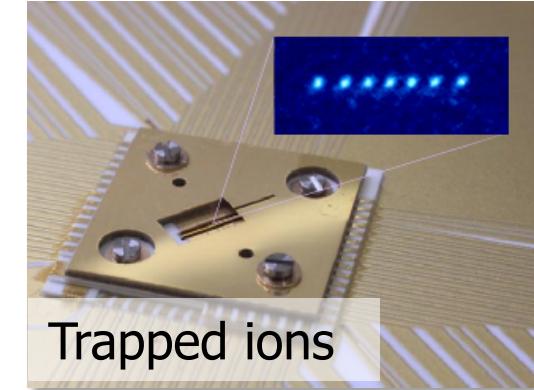
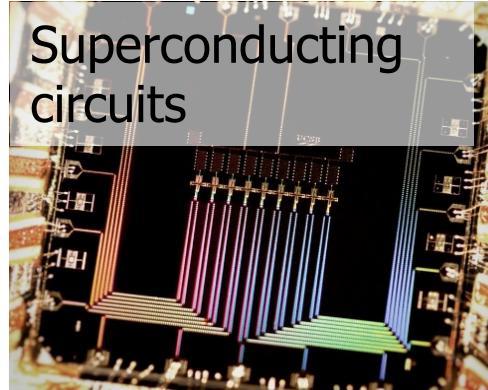
- Spin 1/2
- Defect free chain of spins preparation
- Long lifetime and strong interaction
 - Observe many interaction cycles
- Fully tunable Hamiltonian $H = H_0 + H_{\text{ext}} + H_{\text{int}}$



Quantum simulations: various systems

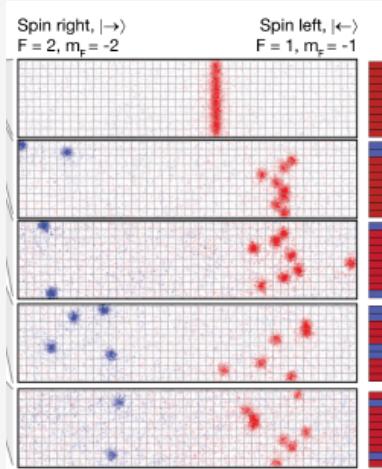


How to simulate?



Present Rydberg atom based quantum simulators

- MOT insulator of ground state atoms + Rydberg dressing



→ dynamic of a linear 10 atom Ising spin chain

→ simulation duration limited by blackbody induced Rydberg losses

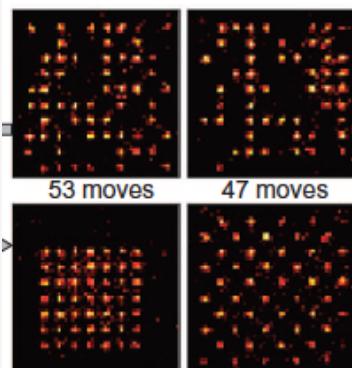
$$\tau_{loss} \approx 130\mu s$$

→ Filling factor smaller than 1

I. Bloch, C. Gross

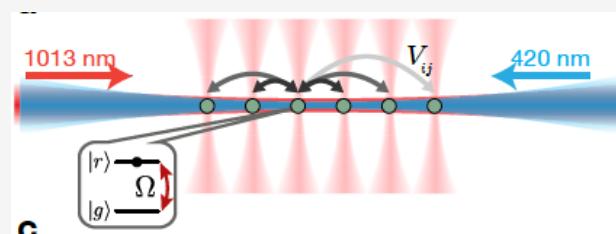
arXiv:1705.08372

- Single trapped ground state atoms in optical tweezers



Science 354,
1021 (2017)
49 atom array

A. Browayes Paris-Saclay



arXiv:1707.04344
51 atom linear trap

M. Lukin Harvard-MIT

The Rydberg state is not trapped → simulation limited to few μs timescale

Rydberg atoms quantum simulator

- Two main limitations for low angular momentum Rydberg states (S, P, D laser accessible levels)

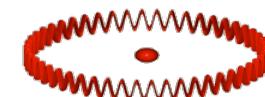
- Finite Rydberg state lifetime (100 μ s for laser accessible states)
 - And blackbody induced transfers
 - Atomic motion
 - An even more severe limitation to the useful time

Reduced but not cancelled by Rydberg dressing of ground states

E. A. Goldschmidt, Phys. Rev. Lett. 116, 113001 (XXX)

- Circular Rydberg atoms ($L=|l|=n-1$)

- Long natural lifetime, 25 ms for $n=48$
 - Spontaneous emission can even be suppressed
 - Large orbit $r_n \sim n^2 a_0$ → Huge electric dipole matrix elements
 - Strong dipole – dipole interactions
 - Can be trapped without ionizing

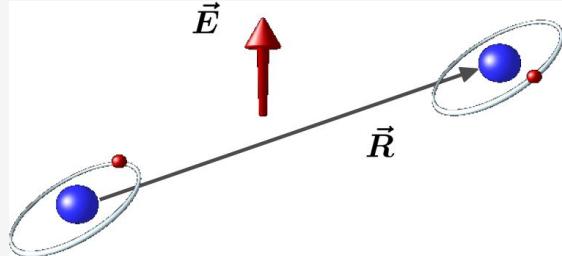


T.L. Nguyen et al, PRX 2018

→ good candidates for building a quantum simulator

Dipole interaction between circular atoms

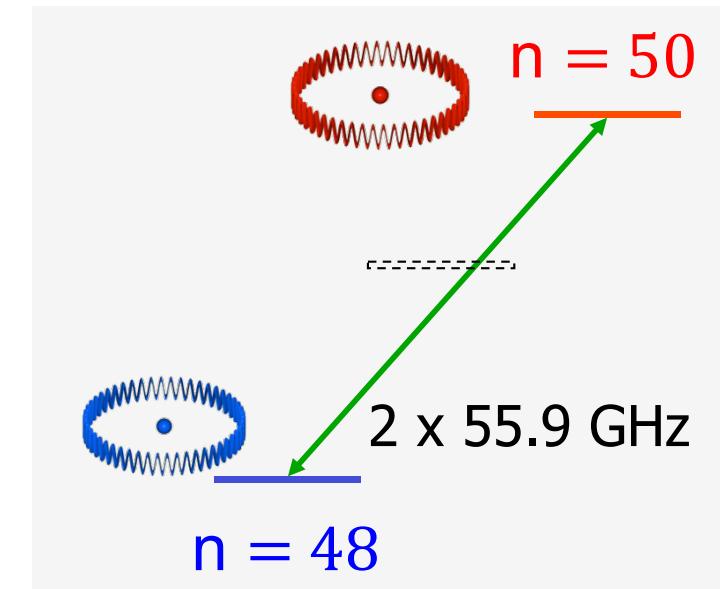
Dipole interaction



$$V_{dd} = \frac{q^2}{4\pi\epsilon_0 r^3} \left(\vec{r}_1 \cdot \vec{r}_2 - 3 \left(\vec{r}_1 \cdot \frac{\vec{r}}{r} \right) \left(\vec{r}_2 \cdot \frac{\vec{r}}{r} \right) \right)$$

$|nC, nC\rangle$ van der Waals interaction $\frac{C_6}{R^6}$
 $|nC, n'C\rangle \Leftrightarrow |n'C, nC\rangle$ exchange interaction

- $n' = n+2$ A_6/R^6 same order of magnitude as vdW

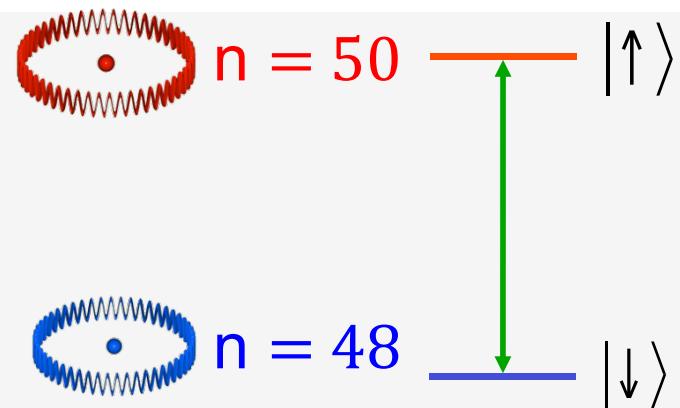
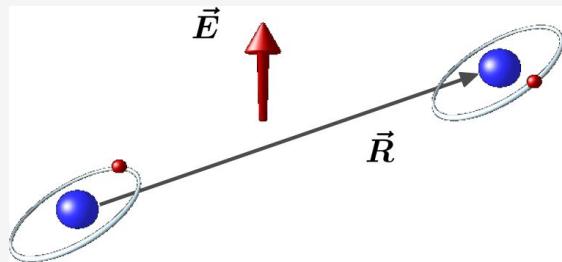


Large $n \rightarrow$ more BB radiation
→ shorter lifetime
Small $n \rightarrow$ lower interaction

→ chose 48C and 50C

XXZ spin chain model

Dipole interaction



Next-neighbor spin chain hamiltonian

$$\frac{H}{\hbar} = \frac{\Delta}{2} \sum_{j=1}^N \sigma_j^Z + \frac{\Omega}{2} \sum_{i=1}^N \sigma_j^X + J_Z \sum_{j=1}^{N-1} \sigma_j^Z \sigma_{j+1}^Z + J \sum_{j=1}^{N-1} (\sigma_j^X \sigma_{j+1}^X + \sigma_j^Y \sigma_{j+1}^Y)$$

X or Z fields
→ result from
microwave dressing:

- $\Delta = \omega_0 - \omega_{\text{mw}}$
- Ω : MW Rabi frequency



Ising

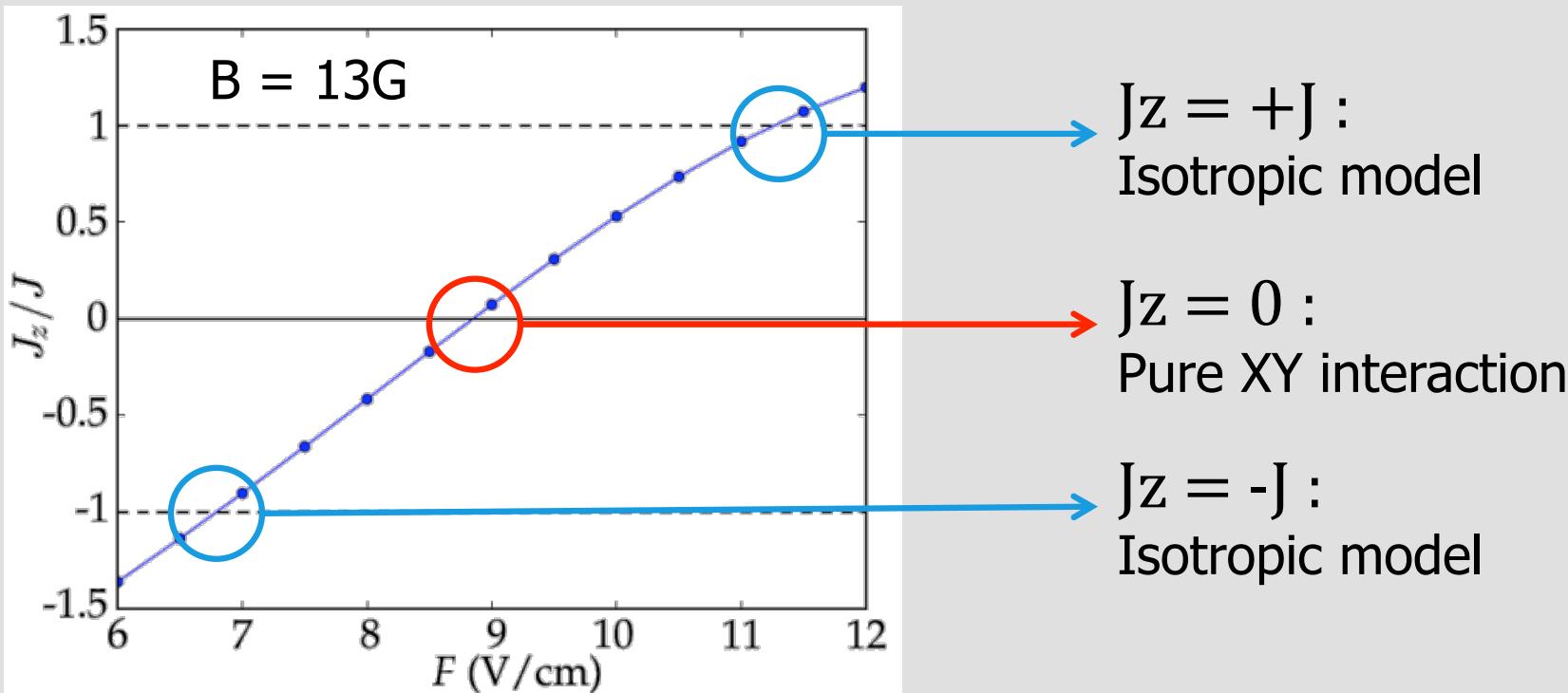
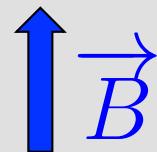
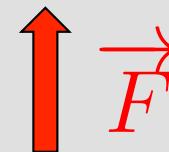
exchange

Tunability of XXZ Hamiltonian

$$\frac{H}{\hbar} = \frac{\Delta}{2} \sum_{j=1}^N \sigma_j^Z + \frac{\Omega}{2} \sum_{i=1}^N \sigma_i^X + J_Z \sum_{j=1}^{N-1} \sigma_j^Z \sigma_{j+1}^Z + J \sum_{j=1}^{N-1} (\sigma_j^X \sigma_{j+1}^X + \sigma_j^Y \sigma_{j+1}^Y)$$

Coupling tunability:

- J nearly constant
- J_z tuned with electric and magnetic fields

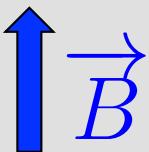
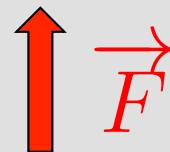
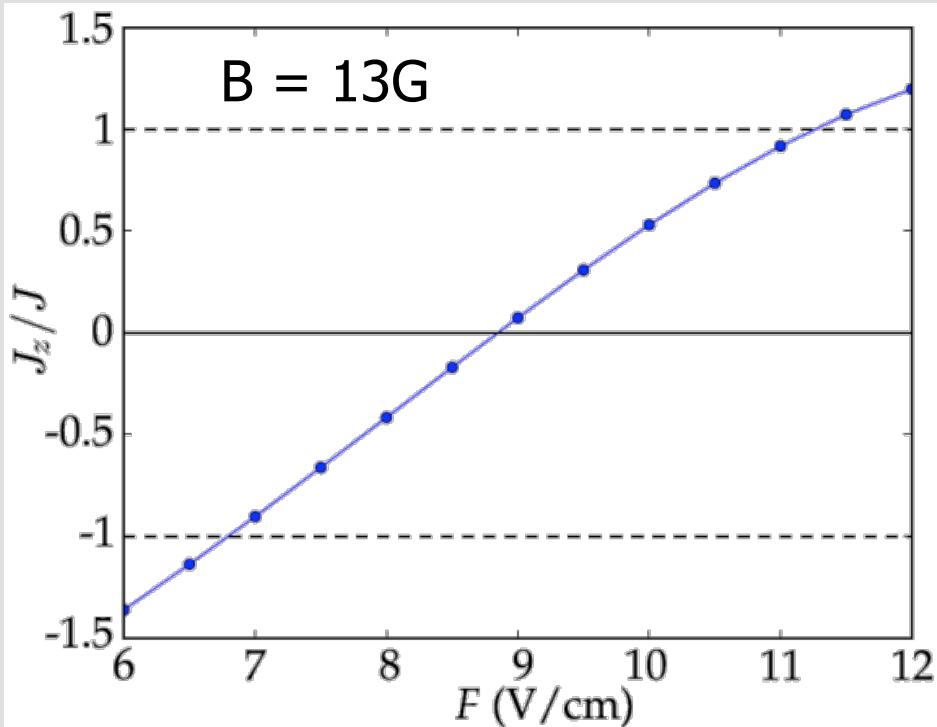


Tunability of XXZ Hamiltonian

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Coupling tunability:

- J nearly constant
- J_z tuned with electric and magnetic fields



- Interaction strength
 - $J = 17 \text{ kHz}$ for $d = 5 \mu\text{m}$,
 - Spin exchange time $1/4J$ in the $10 \mu\text{s}$ range

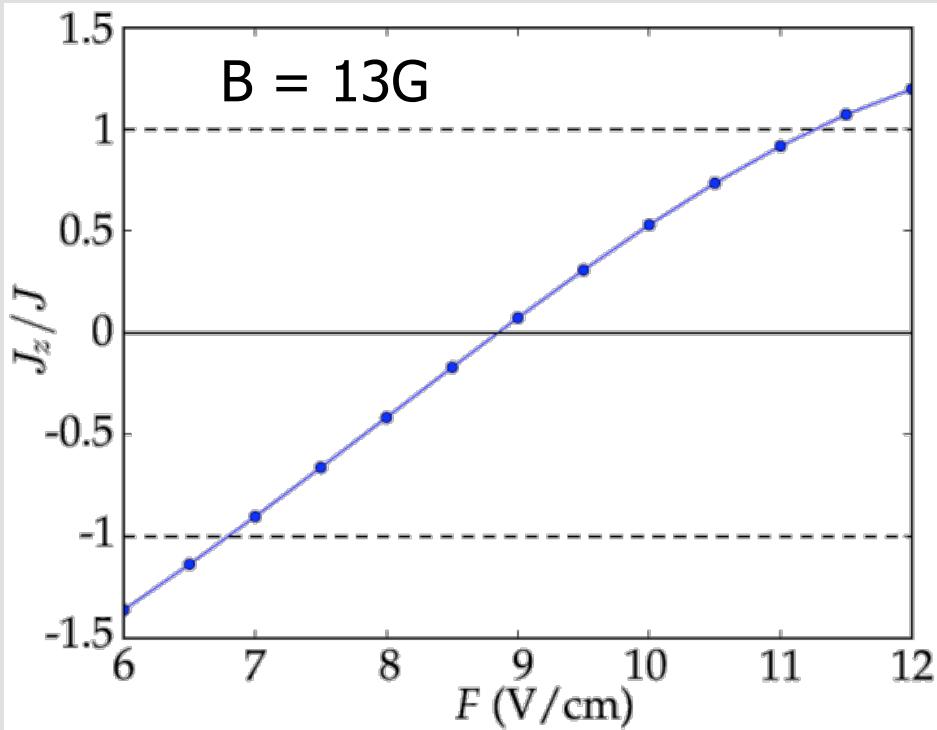
→ Trapping time of 1s
for a 40 atoms chain is
 10^5 exchange times!

Tunability of XXZ Hamiltonian

$$\frac{H}{\hbar} = \frac{\Delta}{2} \sum_{j=1}^N \sigma_j^Z + \frac{\Omega}{2} \sum_{i=1}^N \sigma_j^X + J_Z \sum_{j=1}^{N-1} \sigma_j^Z \sigma_{j+1}^Z + J \sum_{j=1}^{N-1} (\sigma_j^X \sigma_{j+1}^X + \sigma_j^Y \sigma_{j+1}^Y)$$

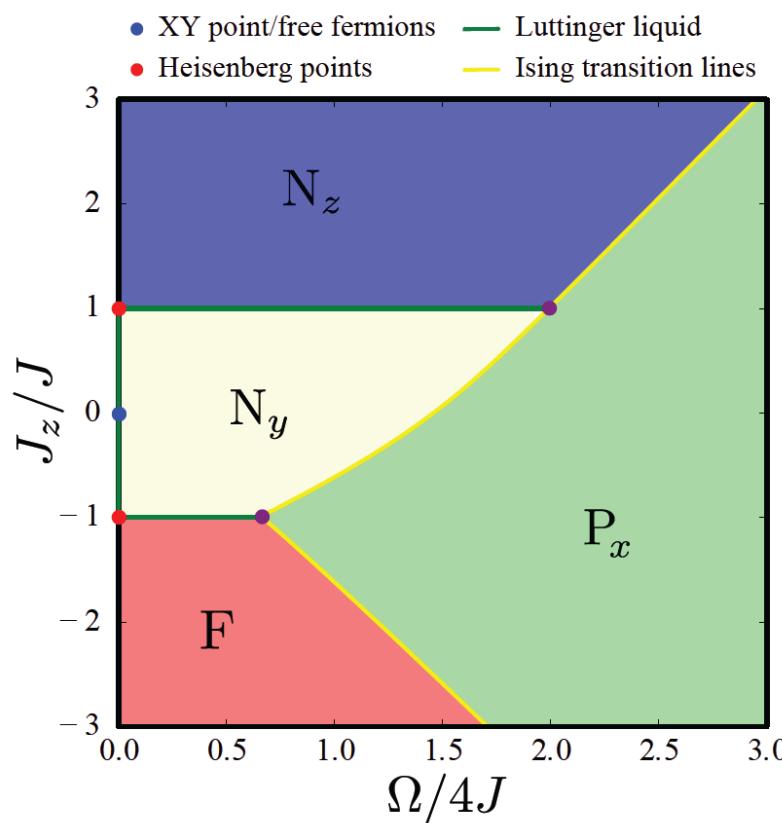
Coupling tunability:

- J nearly constant
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Phase diagram at $\Delta=0$

(Guillaume Roux LPTMS)

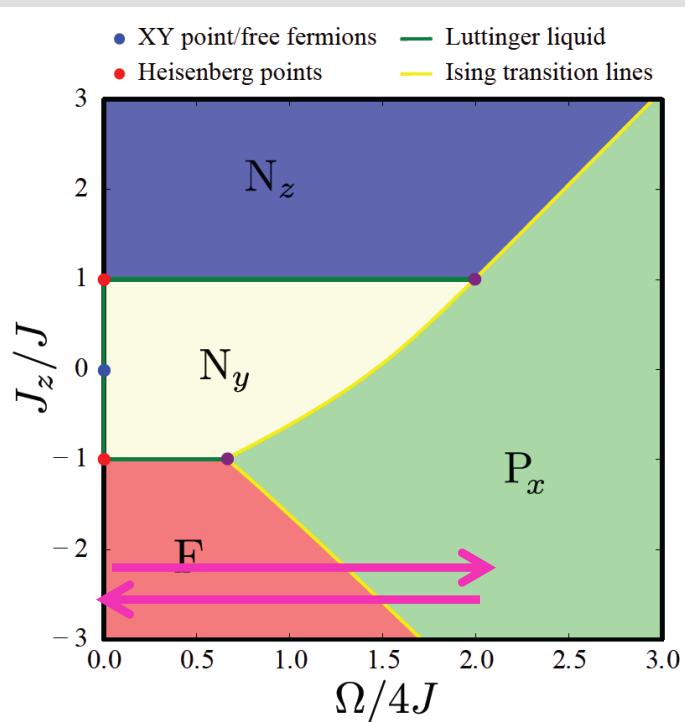


Tunable XXZ spin chain model

Next-neighbor spin chain hamiltonian

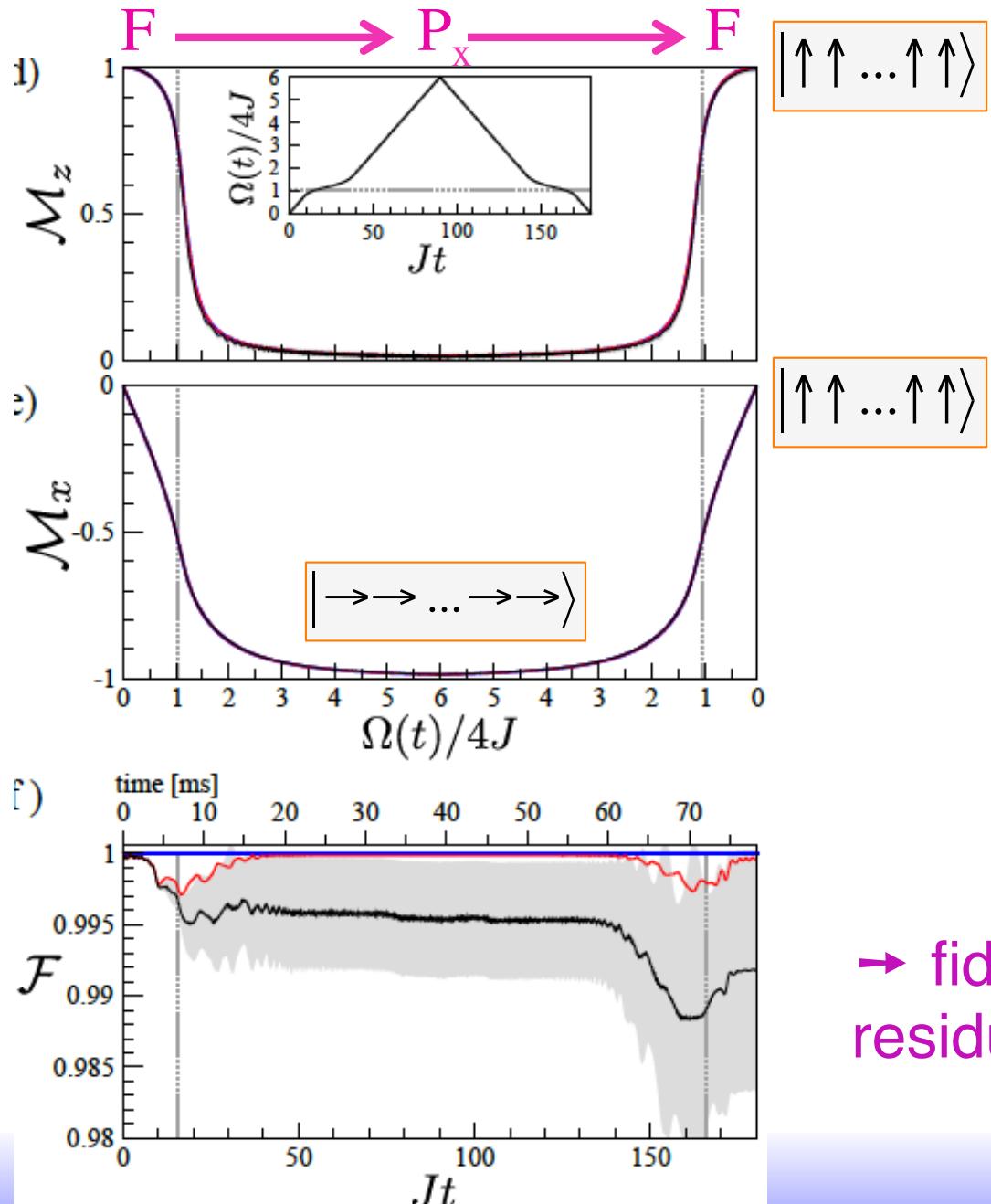
$$\frac{H}{h} = \frac{\Delta}{2} \sum_{j=1}^N \sigma_j^Z + \frac{\Omega}{2} \sum_{i=1}^N \sigma_j^X + J_Z \sum_{j=1}^{N-1} \sigma_j^Z \sigma_{j+1}^Z + J \sum_{j=1}^{N-1} (\sigma_j^X \sigma_{j+1}^X + \sigma_j^Y \sigma_{j+1}^Y)$$

Phase diagram at $\Delta=0$
(Guillaume Roux LPTMS)



→explore phase diagram by adiabatic variation of parameters as a benchmark

Exact simulation of adiabatic phase transitions



Simulation for 14 spin
Including residual motion

$d=7 \mu\text{m}, J=2.3 \text{ kHz}$
Same values of order parameter as in the exact ground state
→ nearly perfect preparation of phase P_x

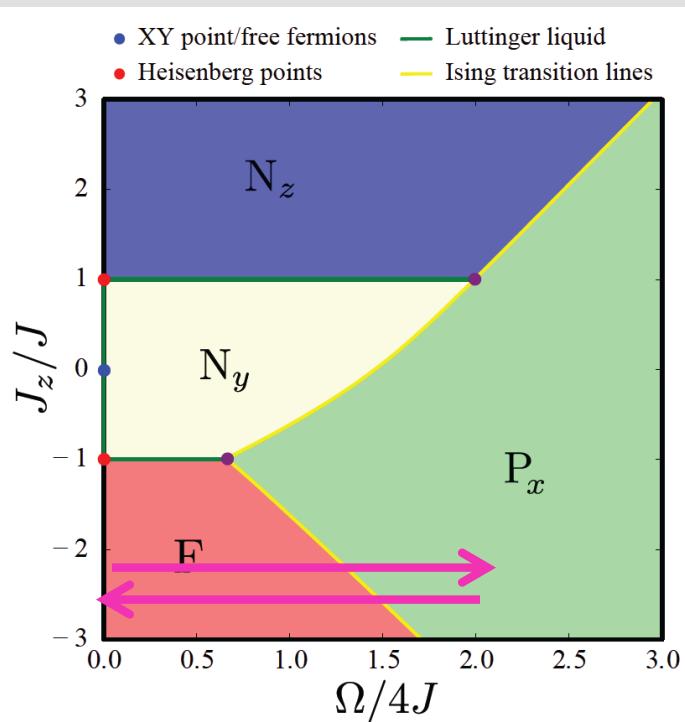
→ fidelity weakly affected by residual atomic motion

Tunable XXZ spin chain model

Next-neighbor spin chain hamiltonian

$$\frac{H}{h} = \frac{\Delta}{2} \sum_{j=1}^N \sigma_j^Z + \frac{\Omega}{2} \sum_{i=1}^N \sigma_j^X + J_Z \sum_{j=1}^{N-1} \sigma_j^Z \sigma_{j+1}^Z + J \sum_{j=1}^{N-1} (\sigma_j^X \sigma_{j+1}^X + \sigma_j^Y \sigma_{j+1}^Y)$$

Phase diagram at $\Delta=0$
(Guillaume Roux LPTMS)



→ explore phase diagram by adiabatic variation of parameters as a benchmark

→ study quenches: defects generation (Kibble-Zurek)

→ study transport: MBL with controlled disorder and interactions

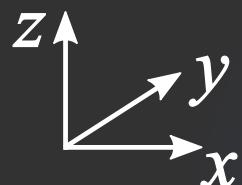
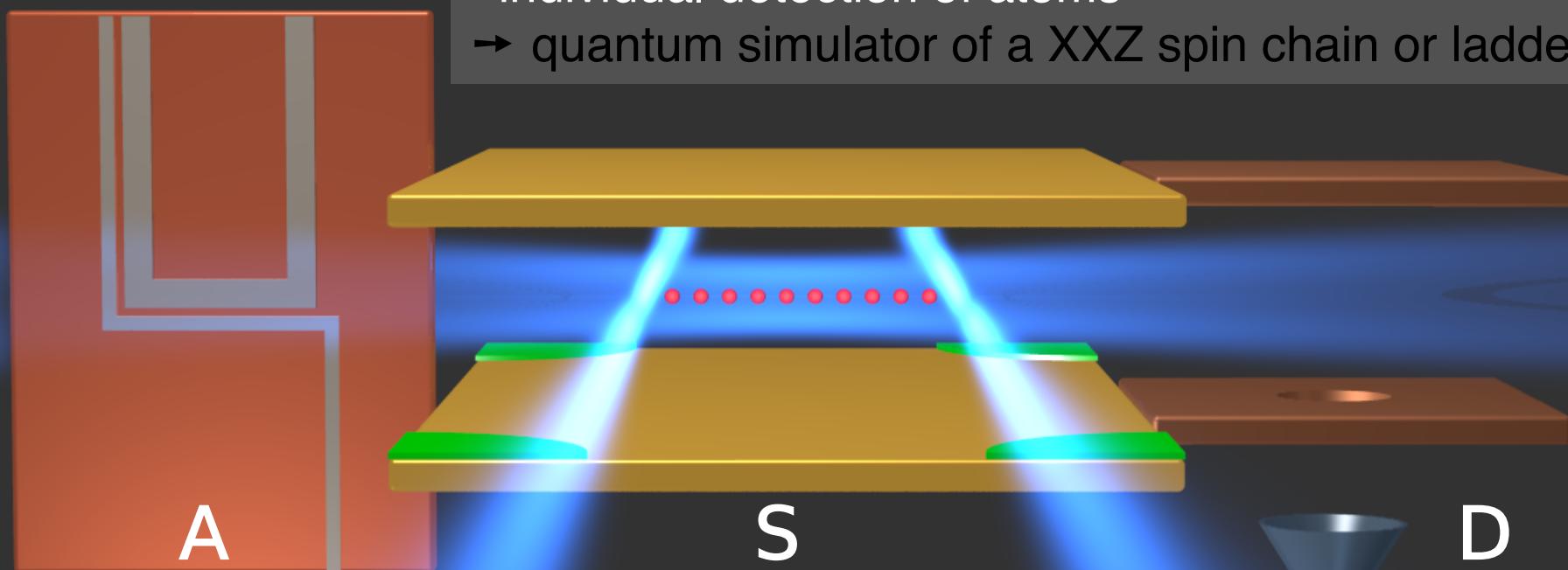
→ spin ladder: study Haldane phase of effective spin 1

...

General scheme of trapped Rydberg atom simulator

Trapped circular Rydberg atoms

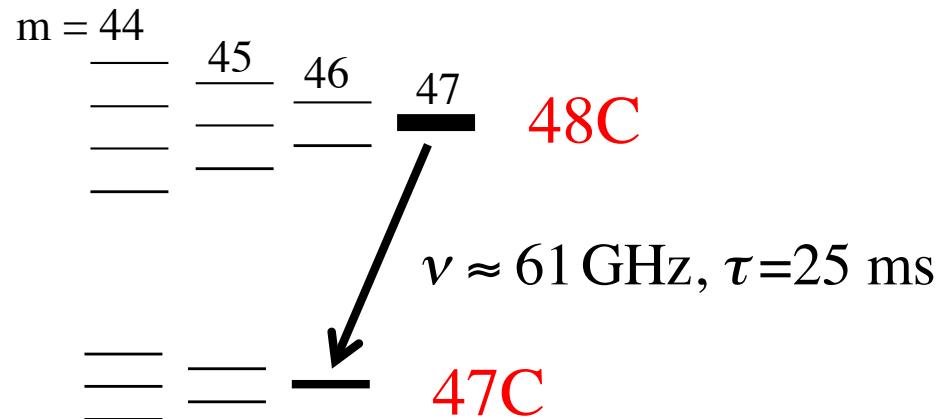
- inhibited spontaneous emission $\tau \approx 1$ min
- ponderomotive laser trap
 - perfect 1D lattice of 40 atoms
- individual detection of atoms
 - quantum simulator of a XXZ spin chain or ladder



Circular Rydberg Atoms (CRA): spontaneous emission inhibition

- CRA decay channel:

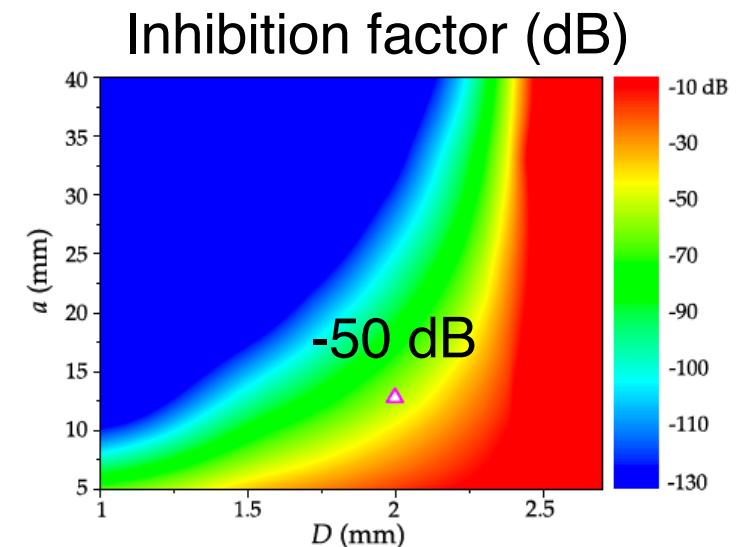
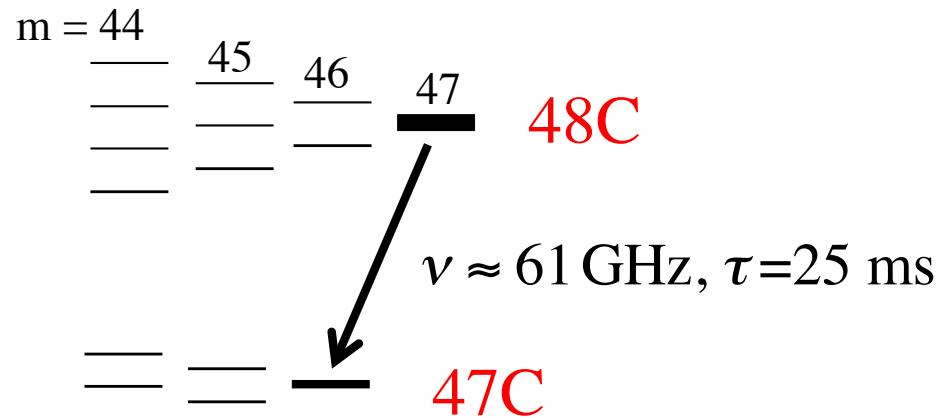
microwave spontaneous emission on a σ^+ transition, **25 ms lifetime for ^{48}C**



Circular Rydberg Atoms (CRA): spontaneous emission inhibition

- CRA decay channel:

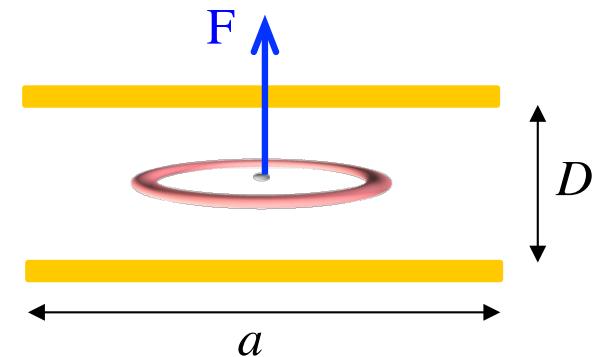
microwave spontaneous emission on a σ^+ transition, **25 ms lifetime for ^{48}C**



- Spontaneous emission inhibition

D. Kleppner Phys. Rev. Lett. 47, 233 (1981)

- Emission inhibited in a capacitor below cut-off.



→ **2500 s life** in a $13 \times 2 \text{ mm}$ capacitor !

laser trapping circular states

S. K. Dutta et al. *Phys. Rev. Lett.* 85, 5551
Raithel group

- Circular states can be laser-trapped !

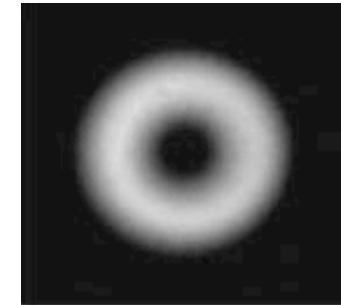
- Ponderomotive electron energy:

- atoms are low-field seekers

- Trapped in vortex beam

- a deep trap

- ~ similar polarizability as ground state Rubidium at $1 \mu\text{m}$ wavelength



- Trapping almost independent of principal quantum number

- Low trap-induced decoherence

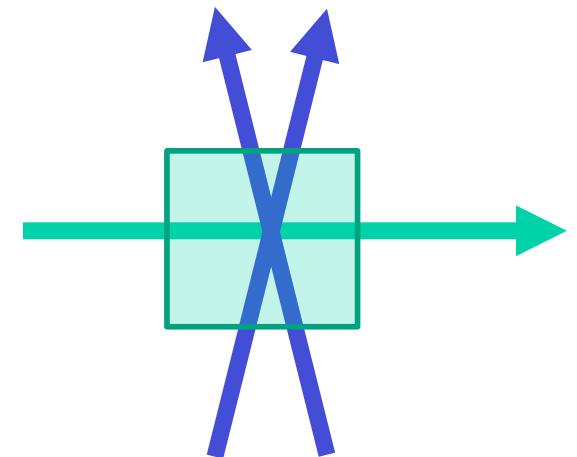
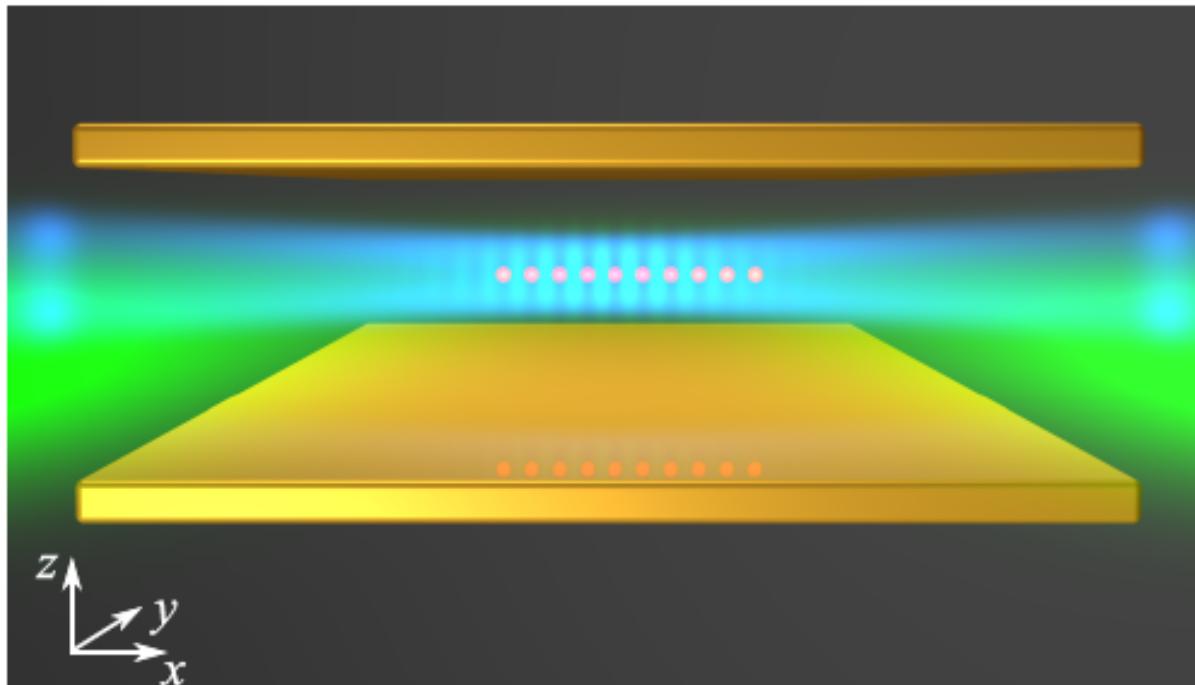
- Impervious to photoionization

- severe limitation for low / states

Saffman et al. Phys. Rev. A 72, 022347

A simple trap geometry for a 1-D lattice

- Trapping lasers at $1 \mu\text{m}$



- LG mode along Ox (transverse trap)
- Two Gaussian beams at a small angle
 - Longitudinal lattice with an adjustable spacing
 - $d = 5$ to $7 \mu\text{m}$
 - 24 kHz longitudinal oscillation frequency

Expected lifetime limit for trapped atoms

Cause	Lifetime (s)
Residual spontaneous emission	2500
Blackbody induced processes	630
Level mixing Two atoms at $d = 5 \mu\text{m}$	88
Dipolar relaxation	∞
Photoionization	∞
Collisions with background gas at 10^{-14} torr	400
Compton elastic diffusion in trap	> 180
Predicted lifetime	47 s

For 50 atoms, less than one atom lost in 1s
This corresponds to 10^4 - 10^5 exchange time

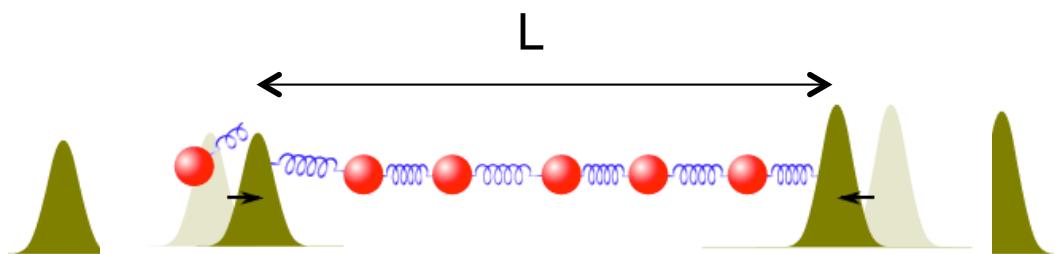
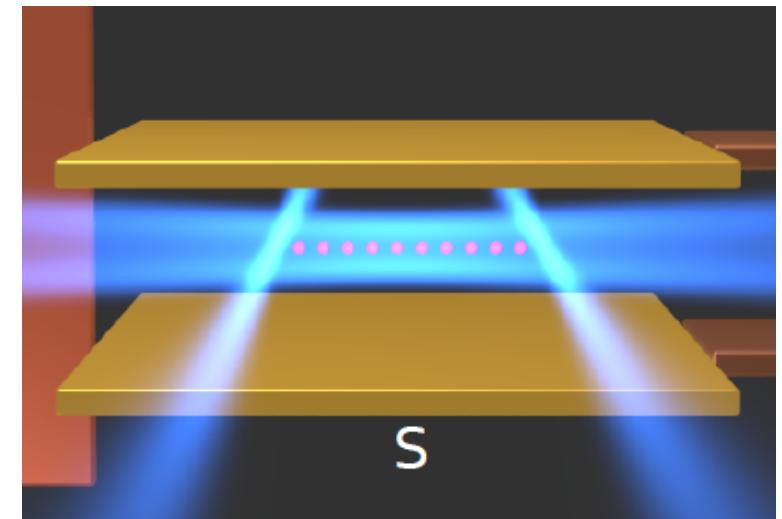
Deterministic chain preparation

- Van der Waals evaporation

- LG and "plug beams trap"
→ One weak, one strong
 - Load ~ 100 circular atoms
 - Compress the trap: atom evaporate
 - Classical simulation

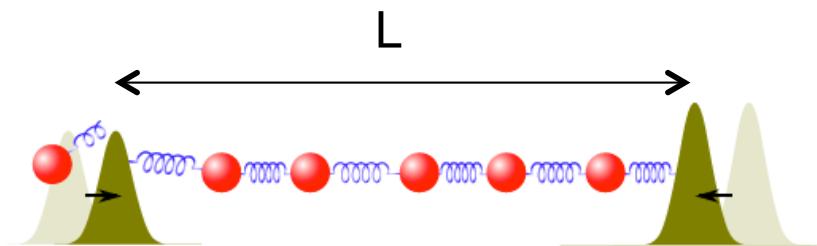
→ Final atom number determined by trap length

Deterministic chain preparation up to ~ 40

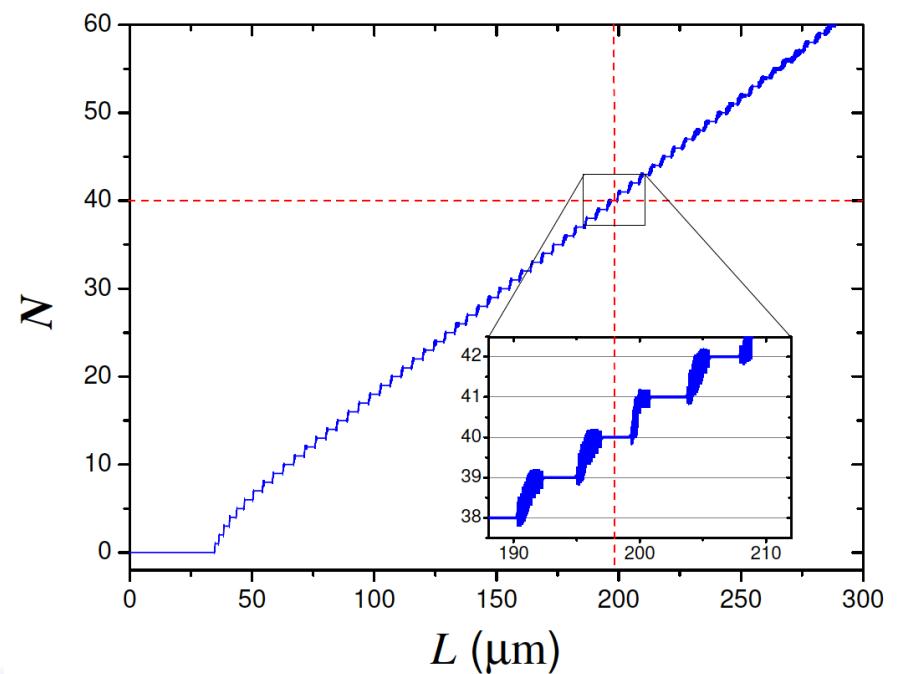
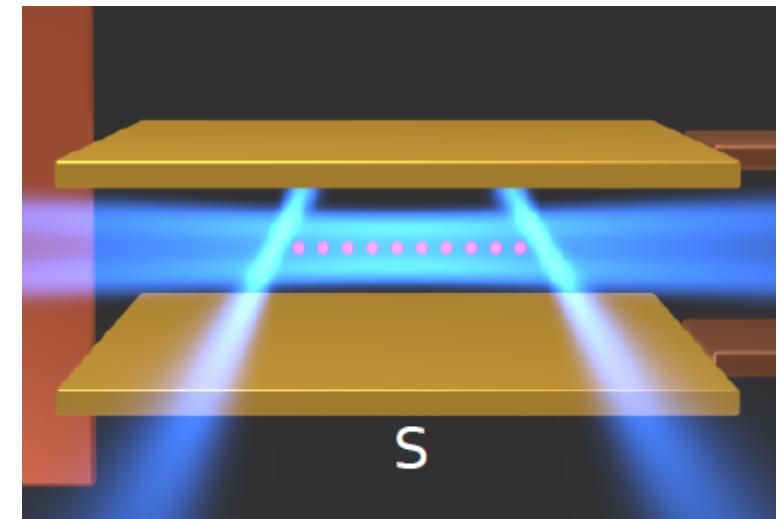


Deterministic chain preparation

- Van der Waals evaporation
 - LG and "plug beams trap"
 - One weak, one strong
 - Load ~ 100 circular atoms
 - Compress the trap: atom evaporate
 - Classical simulation
- Final atom number determined by trap length
Deterministic chain preparation up to ~ 40



→ Efficient evaporative cooling
Final motion amplitude close to ground state



Thermodynamic description: collab. with David Papoulard (Univ. Cergy)

Perspectives for circular atom QS

- Adiabatic exploration of the phase diagram

→ Benchmark

- Adding disorder with a speckle field

- Bose glass physics
 - Many-body localization

- Fast variations of Hamiltonian

- Quenches, Excitation spectroscopy,
 - Floquet engineering

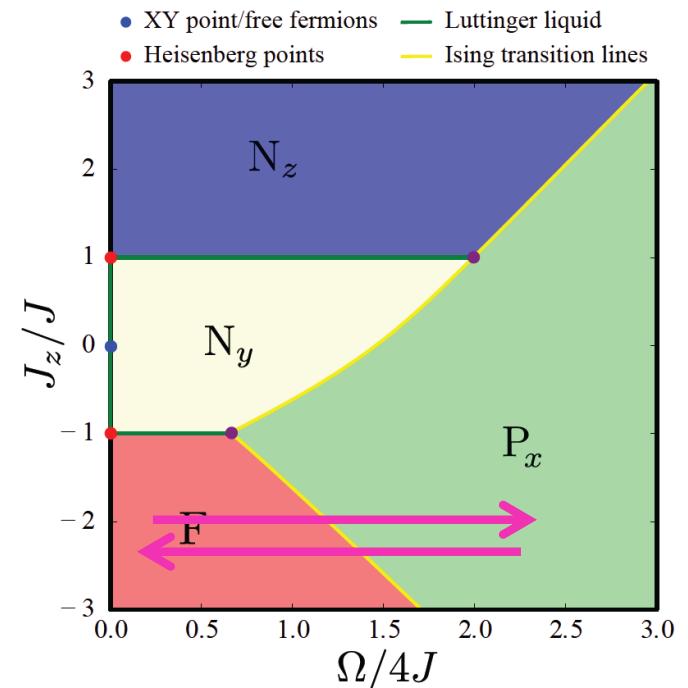
- Study of slow processes: thermalization, spin glass

- In 2D: Ladder geometry and Haldane physics

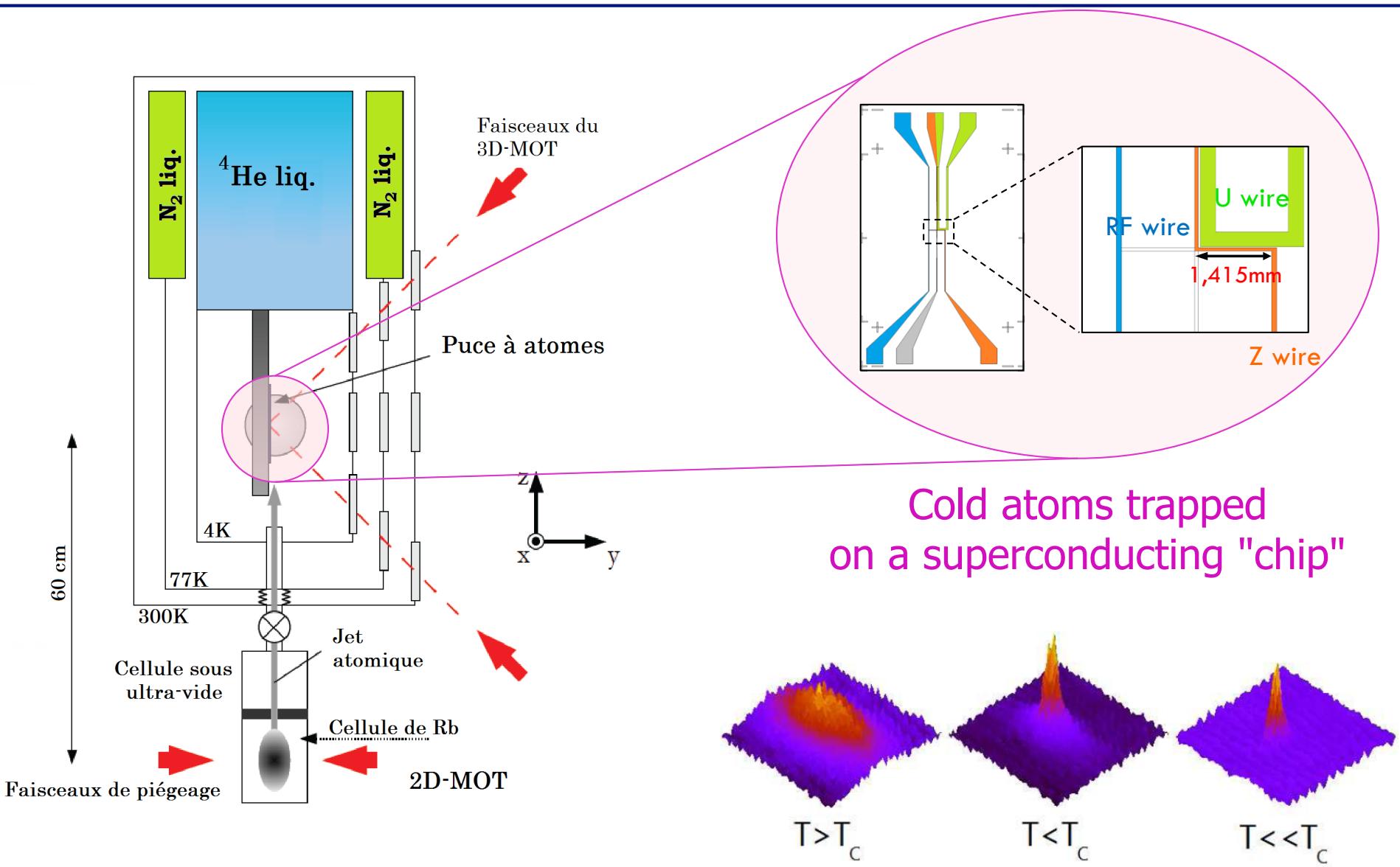
- Bringing two chains together

→ Maps onto Haldane physics: topological order

→ Let us build the circular Rydberg atom simulator



Present experiment: ultracold Rydberg atoms on a chip



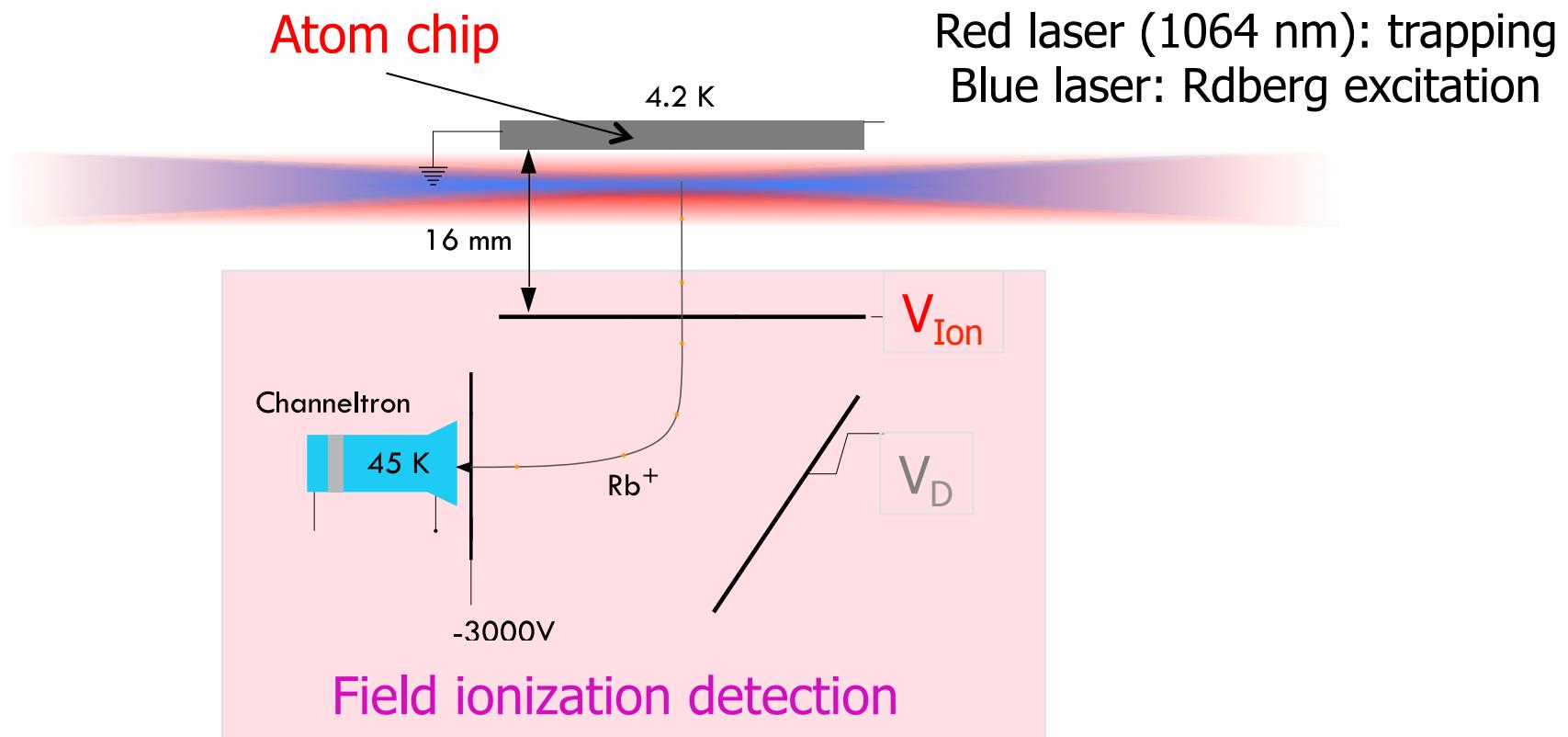
Rubidium atoms

→ evaporative cooling down to 10^4 atom BEC

Roux et al. EPL 81, 56004 (2008)

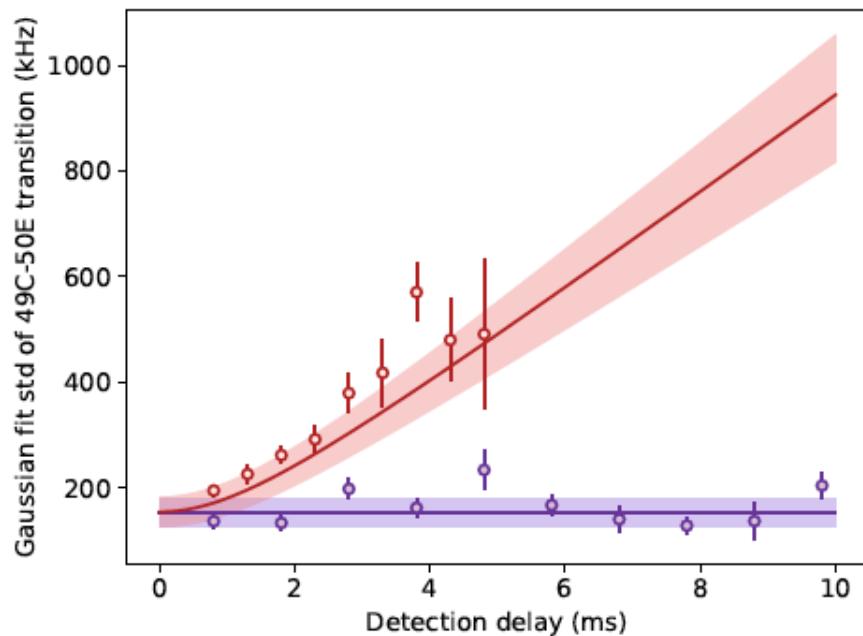
Circular atom trapping: first demonstration

- Microwave spectroscopy in a gradient of electric field:
 - the linewidth of the resonance reflects the spatial extension of the circular atom sample
 - time of fly measurement with and without trapping



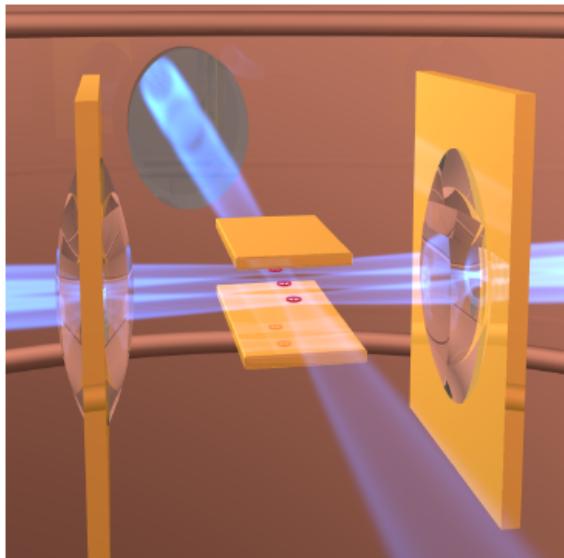
Circular atom trapping: first demonstration

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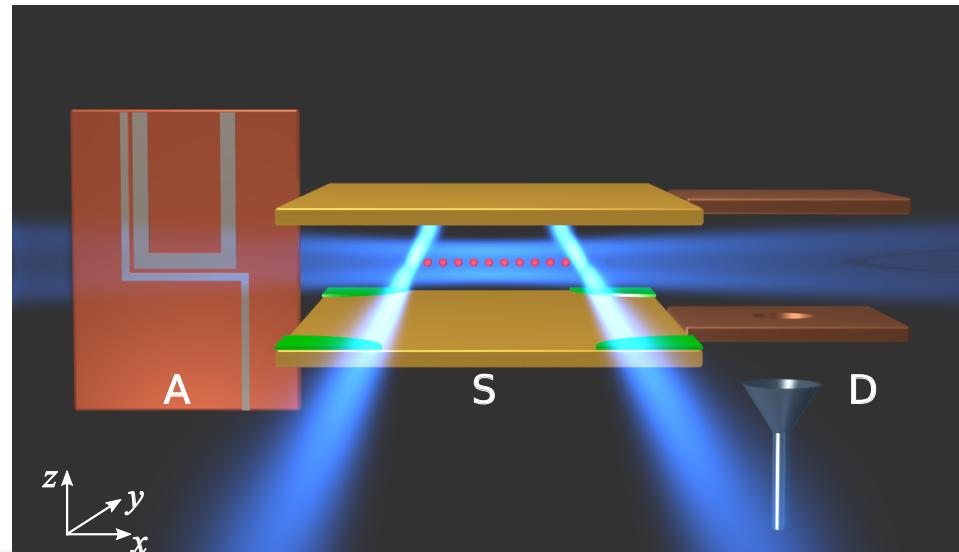


Trapping inhibits
thermal expansion of
circular Rydberg atoms

Trapped Rydberg atoms quantum simulator



1- Simple setup: trapping single CRA in optical tweezers 2D geometry, no control of spontaneous emission



2- Demonstrate 1-10 min inhibition of spontaneous emission for a single trapped atom

3- Put everything together!

The team

+ open post-doc positions...



S. Haroche, M. Brune,
J.M.Raimond,

Cavity QED

I. Dotsenko (two cavity)

S. Gerlich, T. Rybarczyk,
M. Penasa, V. Métillon

S. Gleyzes (slow atoms)

D. Grosso, E.K. Dietsche,
F. Assemat

Superconducting atom chip
Spin simulator

C. Sayrin
Thanh Long Nguyen

T. Cantat-Moltrecht

R. Cortinas
B. Ravon

Quantum metrology

S. Gleyzes
A. Signoles, A. Facon,
E.K. Dietsche, A. Larrouy

Collaborations:

Feedback: P. Rouchon, M.
Mirrahimi, A. Sarlette, Ecole des
Mines Paris

QZD: P. Facchi, S. Pascazio
Uni. Bari

Past Quantum State: K. Mölmer

Spin chain: G. Roux, T.
Jolicoeur, LPTMS

